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DyRoBeS© Manual | **GearLoad**

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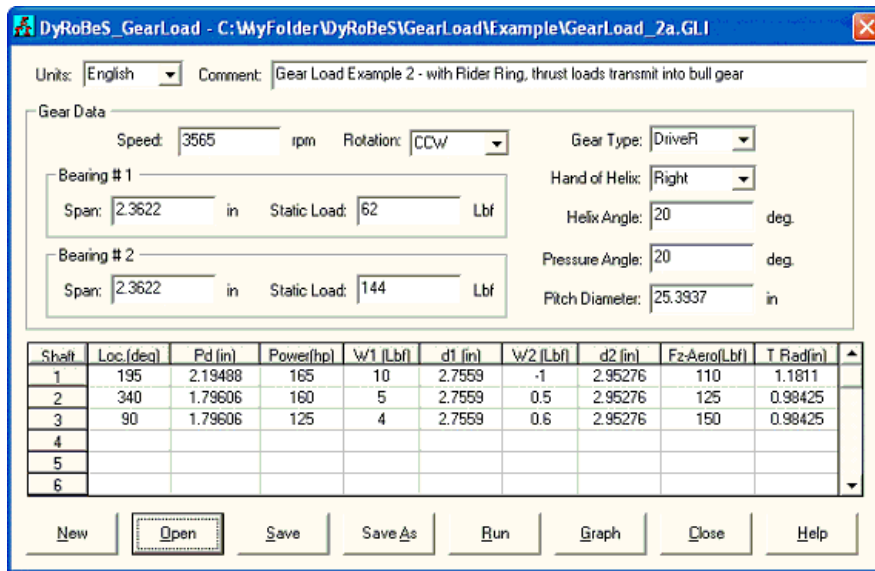
<<DyRoBeS-GearLoad>>

This program calculates the bearing loads due to gear power transmission and aero thrust forces. The gears can be spur gears, helical gears, or double helical gears (herringbone gears). Applications include integrally geared compressors, blowers, pumps, and expanders, etc.. Typical compressor system configuration includes a driver unit (motor, engine, turbine, etc.), which drives several high-speed shafts (driven units) as illustrated in the following figures. Note that in Ver 3.0 of GearLoad program, the Gear can be either a Driver or Driven Gear. For applications like expander or turbine which high-speed expander/turbine will drive the low speed bull gear and the low speed bull gear becomes the driven unit. In that case, the Driver in Figure below will become a Driven unit.
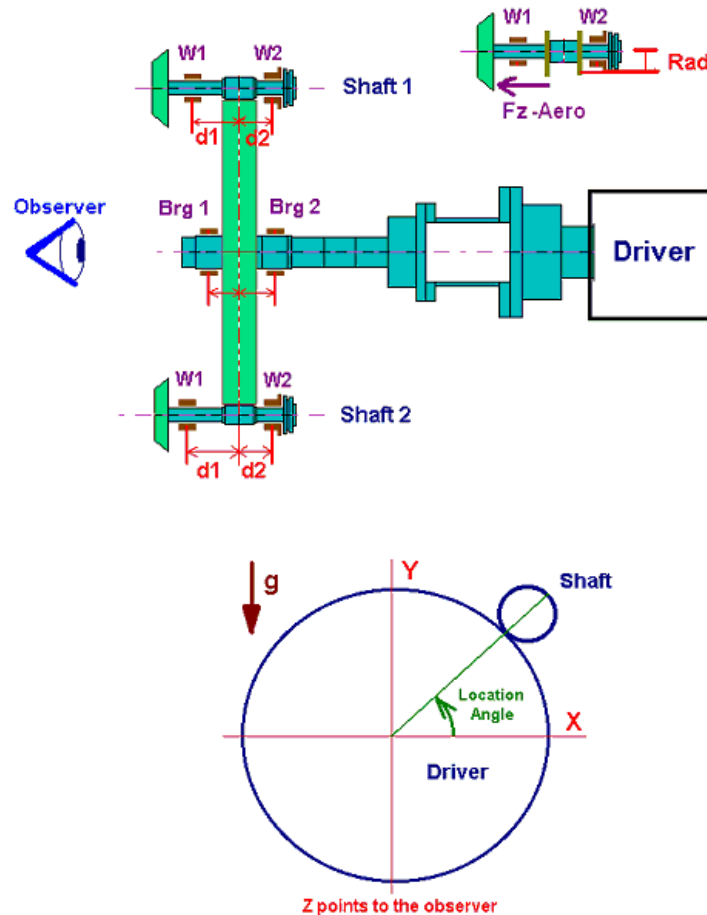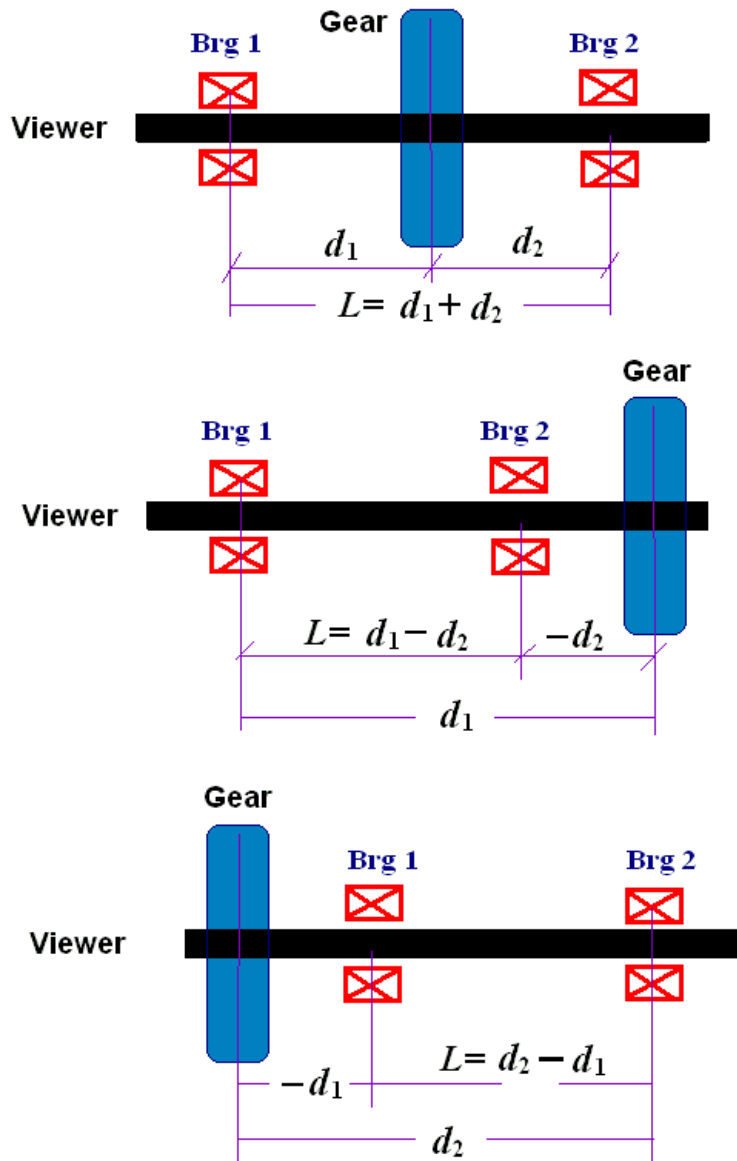

The observer (viewer) can be in either side of the machine, driver side or driven side. The Figure 1 shows that the observer is in the air-side opposite to the driver (motor). The X-axis is to the right of the viewer, Y-axis is to the top, and Z-axis is towards to the viewer, following the right-hand rule. The gravitational force is in the negative Y (-Y) direction. Bearing #1 is the bearing close to the observer and bearing #2 is the bearing away from the observer.

A typical input screen for a 3-stages compressor is shown in Figure 3 and the inputs are self-explanatory as illustrated below:

DyRoBeS_GearLoad - C:\MyFolder\DyRoBeS\GearLoad\Example\GearLoad_2a.GLI

Units: English   Comment: Gear Load Example 2 - with Rider Ring, thrust loads transmit into bull gear

Gear Data

Speed: 3565 rpm   Rotation: CCW   Gear Type: DriveR

Bearing # 1
Span: 2.3622 in   Static Load: 62 Lbf

Bearing # 2
Span: 2.3622 in   Static Load: 144 Lbf

Hand of Helix: Right
Helix Angle: 20 deg.
Pressure Angle: 20 deg.
Pitch Diameter: 25.3937 in

Shaft	Loc.(deg)	Pd (in)	Power(hp)	W1 (Lbf)	d1 (in)	W2 (Lbf)	d2 (in)	Fz-Aero(Lbf)	T Rad(in)
1	195	2.19488	165	10	2.7559	-1	2.95276	110	1.1811
2	340	1.79606	160	5	2.7559	0.5	2.95276	125	0.98425
3	90	1.79606	125	4	2.7559	0.6	2.95276	150	0.98425
4									
5									
6									

[New] [Open] [Save] [Save As] [Run] [Graph] [Close] [Help]

In Ver 3.0, the main gear can be a driver unit or driven unit. For compressor applications, the bull gear (low speed gear) is a driver which drives multiple high speed pinions. For expanders/turbines, the low speed gear can be a driven unit. **Bearing Span** is the distance from the bearing to the center of the gear mesh.

Location angle (**Loc**-deg) specifies the shaft (pinion) angular position relative to the bull gear center, measured from the +X axis. **Pd** represents the Pitch Diameter. **Power** is the stage (pinion) power. **W** is the static load in the negative Y direction. Note that positive W is in the negative Y direction. **d** represents the distance from bearing center to the gear mesh center (bearing span from gear mesh). 1 and 2 represent the bearing numbers 1 and 2. Note that **d1** and **d2** are positive values if the gear is straddle mounted between 2 bearings and the total bearing span (from bearing to bearing) is L= **d1**+**d2**. If gear is overhung mounted outside the bearing span and away from the viewer, then **d1** is positive and **d2** is negative value and L=d1-d2. If gear is overhung mounted outside the bearing span and close to the viewer, then **d1** is negative and **d2** is positive value and L=d2-d1. See figure below for illustration. The **Fz-Aero** is the **aero** force acting on the pinion (stage) centerline. **T-Rad** Is the **radius** where the thrust load will be transmitted to either thrust bearing or rider ring. That is the distance from pinion center to the thrust load vector. For pinions with thrust bearings, **T-Rad** is zero, and the aero forces **Fz-Aero** do not transmit into the bull gear. For pinions with rider ring (thrust collar), **T-Rad** Is the contact point where the pinion net thrust is transmitted into the bull gear. The Net thrust load for each pinion will be the sum of gear force and aero load. The Net thrust load on the bull gear will be the sum of the gear forces and the forces transmitted from rider rings (if it exists).

Gear

Brg 1   Brg 2

Viewer

d_1 d_2

$L = d_1 + d_2$

Brg 1   Brg 2

Gear

Viewer

$L = d_1 - d_2$ $-d_2$

d_1

Gear

Brg 1   Brg 2

Viewer

$-d_1$ $L = d_2 - d_1$

d_2

Outputs for the above input data can be a graphic plot of a text output. The graph is shown below. It contains the bearing load vectors (magnitudes & angles) and each shaft location with respect to the bull gear. It also contains the thrust loads for each rotor. Note that for thrust load, positive is toward the viewer. With rider ring design, the pinion thrust load is the load acting on the low speed bull gear thrust collar from the pinion. The total thrust load on the bull gear will be the summation of these pinion thrust forces and the gear axial forces from each pinion. It will be exactly equal to the total aero loads.

Gear Load Example 2 - with Rider Ring, thrust loads transmit into bull gear
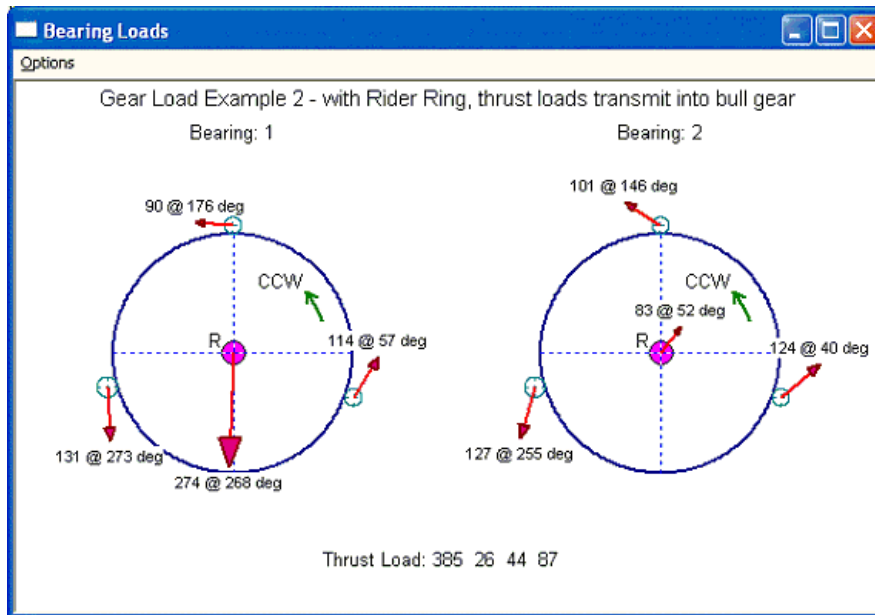
The text outputs are listed below for reference:

```
***** Coordinate System *****
 X-Axis to the right,  Y-Axis to the top,  Z-axis to the Observer
 Gravitational forces applied in the -Y direction
 Angle measured CCW from the +X Axis (Right Hand Rule)

 Brg#1 is the brg closest to the observer
 Brg#2 is the brg farest to the observer

***** System Description *****
 Gear Load Example 2 - with Rider Ring,
 thrust loads transmit into bull gear

*** Reference Shaft Data *****
 Rotational Speed (rpm):    3565.00
 Gear Number...........:       1
 Driver/Driven Gear....:    DRIVER
 Hand of Helix.........:    RIGHT
 Direction of Rotation.:    CCW
 Helix Angle.....(Degs):   20.0000
 Pressure Angle..(Degs):   20.0000
 Pitch Diameter....(in):  25.39370
 Brg#1 Span/gear...(in):   2.36220
 Brg#2 Span/gear...(in):   2.36220

***** Bearing Loads Calculation *****
                         <Reference>....<<Shafts.......---->
 Shaft #...................:                 1         2         3
 Reference Shaft Gear#.....:                 1         1         1
 Angular Location....(Degs):            195.00    340.00     90.00
 Rotational Speed.....(rpm):   3565.00 41245.33  50403.96  50403.96
 Pitch Diameter........(in):            2.19488   1.79606   1.79606
 HorsePower............(hp):    450.00   165.00    160.00    125.00
 Gear Force Components (Lbf)
 Tangential (Work) force...:            229.74    222.78    174.05
 Radial (Separating) force.:             88.99     86.29     67.41
 Axial (Thrust) force......:            -83.62    -81.09    -63.35
 Fx........................:            -26.49    157.28   -174.05
 Fy........................:           -244.95    179.83     67.41
 Fz........................:            -83.62    -81.09    -63.35
 External Load (Aero Load)
     Axial Aero Load (Lbf):            110.00    125.00    150.00
        Thrust At Radius (in):        1.18110    .98425    .98425

 Brg#1 Static Load....(Lbf):   62.0000  10.0000    5.0000    4.0000
        Span/Gear tooth.(in):           2.7559    2.7559    2.7559
        Load (X-dir)...(Lbf):  -8.1950   7.0965   62.2517  -90.0251
        Load (Y-dir)...(Lbf): -273.6786 -131.1237  94.9698    5.9641
        Load (mag.)....(Lbf):  273.8013 131.3155  113.5541   90.2225
        Load (angle)..(Degs):   268.28    273.10     56.76    176.21

 Brg#2 Static Load....(Lbf):  144.0000  -1.0000     .5000     .6000
```

```
    Span/Gear tooth.(in):                2.9528     2.9528     2.9528
    Load (X-dir)...(Lbf):     51.4537   -33.5887    95.0302   -84.0232
    Load (Y-dir)...(Lbf):     65.3779  -122.8232    79.3638    56.8499
    Load (mag.)....(Lbf):     83.1971   127.3332   123.8117   101.4485
    Load (angle)..(Degs):       51.80     254.71      39.87     145.92

  Thrust Brg Loads.....(Lbf):  385.0000    26.3801    43.9140    86.6516
  Force acting on the Thrust Brgs
  Thrust on bull gear brg is the sum of total Aero loads
  Thrust on pinion is the force acting on the rider ring
  Aero thrusts from pinions are transmitted to bull gear
 ***** End of Analysis *****
```

Convenient Unit Conversations:

mm = 25.4 * in

N = 4.448222 * Lbf

kgf = 0.4535924 * Lbf

N = 9.8066 * kgf

KW = 0.7457 * hp

Bearing Load Calculation

The bearing load calculation is very straightforward and based on the force and moment balance equations. The forces and moments are balanced for the entire machine, also for each individual rotor. For the entire machine, the forces include bearing reaction forces, gravity (static loads), and aero loads if exist. The gear forces are internal forces and not considered in the entire machine free-body diagram. For each individual rotor, the gear forces must be considered. It should be kept in mind that the gear forces (tangential, radial, and axial) acting on the driven gear are always directly opposite acting on the driver gear to meet the action-reaction relationship.

Gear Forces

The gear force contains 3 components, that is tangential (work) force, radial (separation) force, and axial (thrust) force. Since the power is typically given, the tangential force component is obtained from the power and torque relation:

Power = Torque X Velocity = (rp X Ft) X = Ft X (rp)

where Ft is the tangential force, rp is the pitch radius, and is the rotational velocity in (rad/sec).

In English units:

$$|F_t| = \frac{60 \times 6600}{2\pi}\left(\frac{hp}{rpm \times r_p}\right) = \frac{63025 \times hp}{rpm \times r_p}$$

where Ft is in Lbs, hp = horsepower, rpm is the rotational speed, and rp is in inches.

In metric units:

$$|F_t| = \frac{60 \times 10^6}{2\pi}\left(\frac{kW}{rpm \times r_p}\right)$$

where Ft in Newton, power is kW, and pitch radius in mm. The magnitude of the radial force is:

$$|F_r| = \frac{|F_t|\tan\phi_p}{\cos\phi_h}$$

where ϕ_h and ϕ_p are the helix angle and pressure angle, respectively. And the magnitude of the axial force is:

$$|F_a| = |F_t|\tan\phi_h$$

For spur gear and double helical gears, the axial force is null. The directions of the tangential and radial force components are easy to understand. Consider the forces on the **driven** gear flank at the contact point, four cases are studied and shown below. The tangential force component is always along the direction

of rotation and the radial force component is from the contact point toward the driven gear center. Without the helical angle ($\phi_h = 0$), the resulting force is always along the pressure line ($\tan \phi_p = \dfrac{|F_r|}{|F_t|}$). Again, the forces acting on the driver gear will be exactly opposite from the force acting on the driven gear.

Force on the Driven Gear
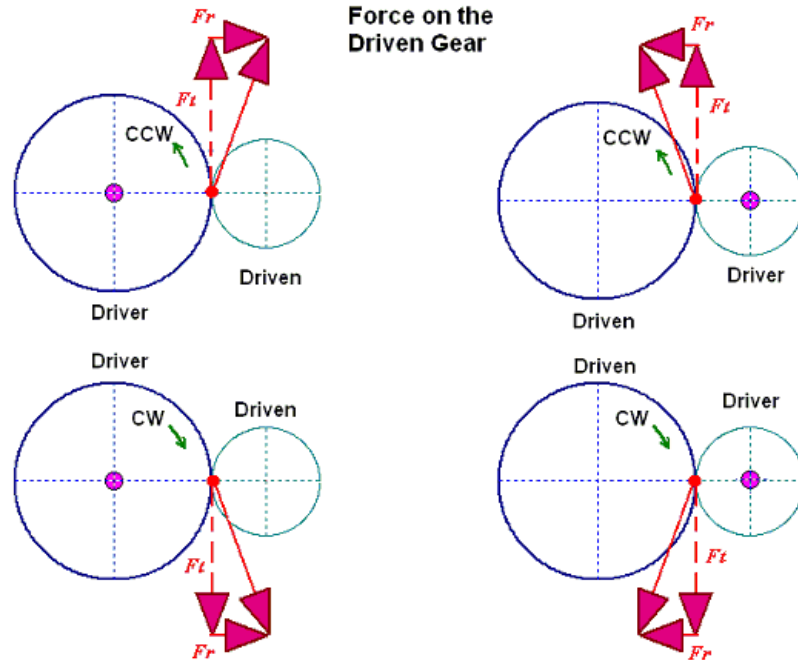
The magnitudes and directions of the tangential and radial forces are determined from the above discussion. It is necessary to transform the tangential and radial forces into a standard Cartesian coordinates (x, y) system for the following bearing load calculation, as shown in the figure. The transformations are given below:

$$\hat{e}_r = \hat{i} \cos \theta + \hat{j} \sin \theta$$
$$\hat{e}_t = -\hat{i} \sin \theta + \hat{j} \cos \theta$$

$$\hat{i} = \hat{e}_r \cos \theta - \hat{e}_t \sin \theta$$
$$\hat{j} = \hat{e}_r \sin \theta + \hat{e}_t \cos \theta$$

$$F_x = F_r \cos \theta - F_t \sin \theta$$
$$F_y = F_r \sin \theta + F_t \cos \theta$$

Force on driven gear

unit vectors
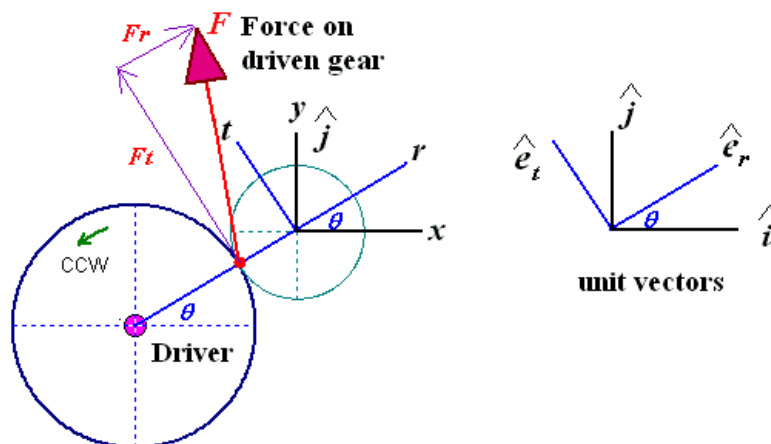
The direction of the axial force is described in the following table when viewing from the axis of rotation.

| Hand of Helix	Rotation	Driver	Driven
Right	CCW	Toward viewer (+Z)	Away from viewer (-Z)
Right	CW	Away from viewer (-Z)	Toward viewer (+Z)
Left	CCW	Away from viewer (-Z)	Toward viewer (+Z)
Left	CW	Toward viewer (+Z)	Away from viewer (-Z)

Before we discuss the bearing load calculation, let us look at two typical configurations for the high-speed pinions. One has a thrust bearing in the pinion to carry the thrust load and the other utilizes a thrust collar (sometimes called rider ring) to transfer the thrust load into the low speed gear for lower mechanical power loss, as illustrated in the following two figures. Both viewed from the impeller side into the driver (motor). The bull gear rotates CCW with right hand of helix. For the configuration with a thrust bearing, the aero load is in the positive Z direction and gear axial force is in the negative Z direction. The forces shown in the figures are the forces acting on the pinion rotor only. The net thrust load (aero load – gear axial force) is carried by a thrust bearing in the pinion itself. Since the gear axial force satisfies the action-reaction relation, this force is also acting on the low speed gear and not shown in the figure. The second configuration with thrust collars in both sides of the pinion and pinion does not have a thrust bearing. The net thrust load is now acting on the low speed bull gear through the thrust collar.

Axial Forces on Pinion

Axial Force Balance

$$\text{Aero Load} = \text{Gear Axial Force} + \text{Thrust Load on Collar}$$
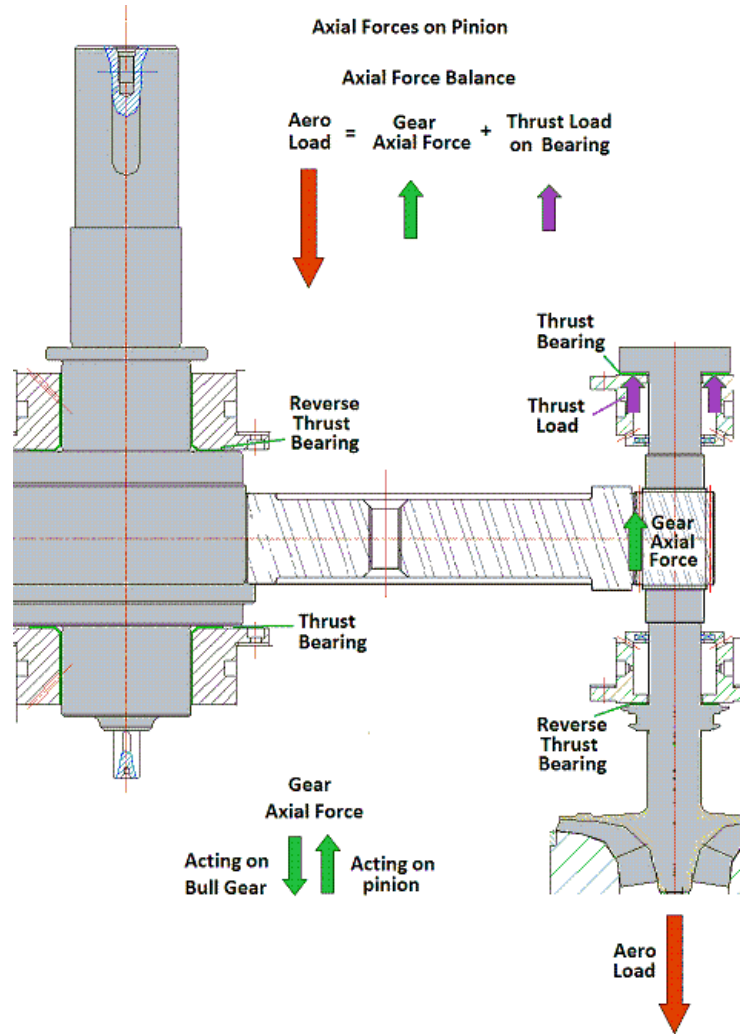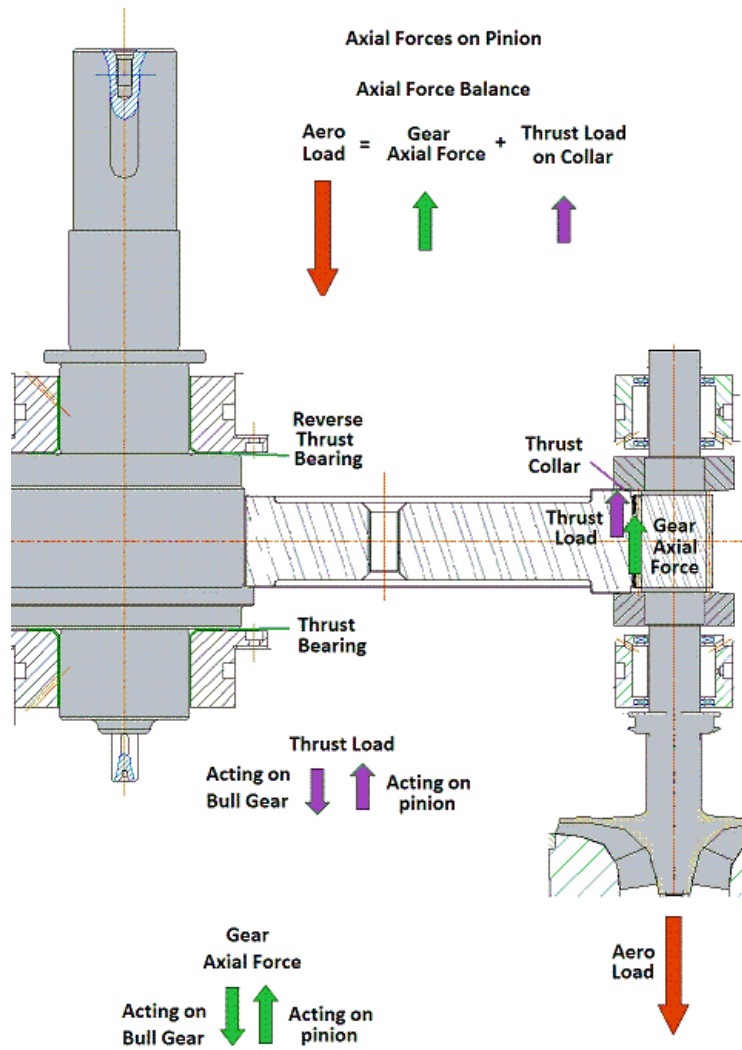
For the bearing load calculation, let us examine the free-body diagram of a typical pinion as shown in the following figure.
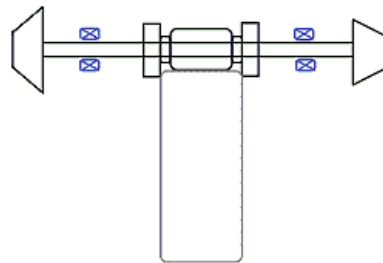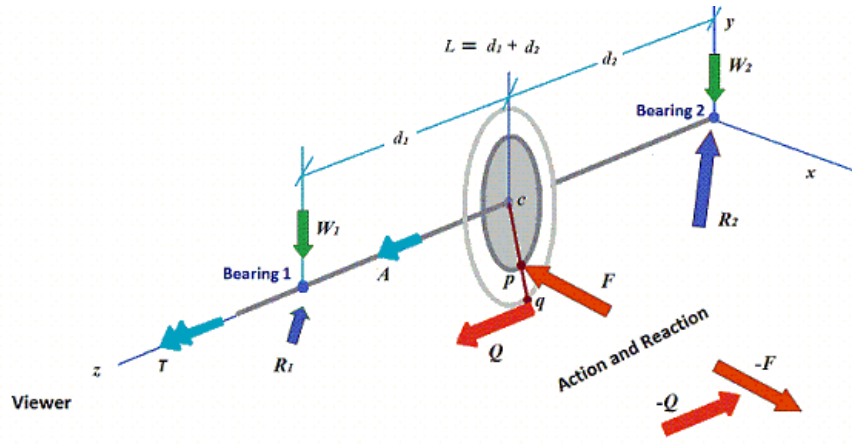
Bearing 1 is the bearing closer to the viewer and bearing 2 is the bearing away from the viewer. T is the torque. $W1$ and $W2$ are the static loads on the bearings, respectively. A is the total aero load. F is the gear force action at the gear contact point p on the pinion. The bull gear will have a reaction gear force with the same magnitude and opposite direction. Q is the thrust load from the thrust collar at the collar contact point q. Typically there is a small taper angle in the collar, 1-5 degrees. Since it is very small, we may assume the Q is along the Z axial only. If the pinion has thrust collar, then the bull gear will have a $-Q$ force acting on the collar contact point. If a thrust bearing is used in the pinion, then Q will be the thrust load on the bearing and it will not be acting on the bull gear. $R1$ and $R2$ are the radial bearing reaction forces acting on the rotor. The unknown reaction forces acting on the pinion are:

$$R_1 = R_{1x}\hat{i} + R_{1y}\hat{j}$$

$$R_2 = R_{2x}\hat{i} + R_{2y}\hat{j}$$

$$Q = Q_z\hat{k}$$

The known gear force, static loads, and net aero load are:

$$F = F_x\hat{i} + F_y\hat{j} + F_z\hat{k}$$

$$W_1 = -W_1\hat{j}$$

$$W_2 = -W_2\hat{j}$$

$$A = A_z\hat{k}$$

For the force balance, we have $\sum F = 0$. The x, y, and z components are:

X: $\quad R_{1x} + R_{2x} + F_x = 0$

Y: $\quad R_{1y} + R_{2y} + F_y - W_1 - W_2 = 0$

Z: $\quad Q_z + F_z + A_z = 0$

For the moment balance, the total moment about bearing 2 is zero.

$$\sum M_2 = 0 = \hat{T} + \hat{r}_{2p} \times \hat{F} + \hat{r}_{2q} \times \hat{Q} + \hat{r}_{21} \times (\hat{R}_1 + \hat{W}_1)$$

where $\hat{T}$ is the torque on the impeller, and $\hat{r}_{2p}, \hat{r}_{2q}, \hat{r}_{21}$ are the displacement vectors from bearing 2 to the gear contact point p, and collar contact point q, and bearing 1 position.

$$\hat{r}_{2p} = d_2\hat{k} + r_p(-\hat{e}_r) = d_2\hat{k} + r_p(-\cos\theta\,\hat{i} - \sin\theta\,\hat{j}) = -r_p\cos\theta\,\hat{i} - r_p\sin\theta\,\hat{j} + d_2\hat{k}$$

$$\hat{r}_{2q} = d_q\hat{k} + r_q(-\hat{e}_r) = d_q\hat{k} + r_q(-\cos\theta\,\hat{i} - \sin\theta\,\hat{j}) = -r_q\cos\theta\,\hat{i} - r_q\sin\theta\,\hat{j} + d_q\hat{k}$$

$$\hat{r}_{21} = L\hat{k} = (d_1 + d_2)\hat{k}$$

and the toque is about the axis of rotation:

$$\hat{T} = T_z\hat{k}$$

where $d2$ is the distance measured from bearing 2 to the center of the gear mesh in the positive Z direction. Therefore, if the gear is mounted in the outside the bearing span and away from the viewer, then $d2$ is a negative value. dq is the distance measured from the bearing 2 to the contact point of rider ring (collar) in the positive Z direction, it is typically equal to $d2$ plus or minus half of the gear face width, depending on the direction of the net thrust load. However, since the net thrust load is in parallel with the axis of rotation (Z axis), it will be shown later that dq is irrelevant to the calculation. rp is the pitch radius of the gear where the gear force F is applied and rq is the radius of the rider ring where the net thrust load Q is applied. Note if a thrust bearing is used in the pinion, then $rq = 0$ and no moment is generated from this net thrust load. Note that $(-\hat{e}_r)$ radial vector, it is because the pinion location is specified based on the bull gear. The contact point is in the negative radial direction for the pinion and positive direction for the bull gear. $r21$ is the distance from bearing 2 to bearing 1. Expand the moment equation, we have:

$$\sum M_2 = 0$$
$$= T_z\hat{k} + (-r_p \sin\theta\, F_z - d_2F_y)\hat{i} + (d_2F_x + r_p\cos\theta\, F_z)\hat{j} + (-r_p\cos\theta\, F_y + r_p\sin\theta\, F_x)\hat{k}$$
$$+ (-r_q\sin\theta\, Q_z)\hat{i} + (r_q\cos\theta\, Q_z)\hat{j} + (-L(R_{1y} - W_1))\hat{i} + (LR_{1x})\hat{j}$$

In X, Y, and Z components:

X: $(-r_p\sin\theta\, F_z - d_2F_y) + (-r_q\sin\theta\, Q_z) + (-L(R_{1y} - W_1)) = 0$

Y: $(d_2F_x + r_p\cos\theta\, F_z) + (r_q\cos\theta\, Q_z) + (LR_{1x}) = 0$

Z: $T_z + (-r_p\cos\theta\, F_y + r_p\sin\theta\, F_x) = 0$

From the moment about Z axis, we have the torque balance equation:

$$T_z = r_p(\cos\theta\, F_y - \sin\theta\, F_x) = r_p F_t$$

Now, we have 5 unknowns ($R_{1x}, R_{1y}, R_{2x}, R_{2y}, Q_z$) and 5 linear algebra equations ($\sum F_x = 0, \sum F_y = 0, \sum F_z = 0, \sum M_x = 0, \sum M_x = 0$).

$$\sum F_z = 0 \Rightarrow Q_z = -F_z - A_z$$

$$\sum M_y = 0 \Rightarrow R_{1x} = \frac{-1}{L}(d_2F_x + r_p\cos\theta\, F_z + r_q\cos\theta\, Q_z) \quad \sum M_x = 0 \Rightarrow R_{1y} = \frac{-1}{L}(r_p\sin\theta\, F_z + d_2F_y + r_q\sin\theta\, Q_z) + W_1$$

$$\sum F_x = 0 \Rightarrow R_{2x} = -R_{1x} - F_x$$

$$\sum F_y = 0 \Rightarrow R_{2y} = -R_{1y} - F_y + W_1 + W_2$$

Once these 5 reactions forces are found, the bearing loads have the same magnitude and opposite directions. The radial loads can be used to determine the equilibrium position of the bearings and linearization of the bearing coefficients. The thrust load Qz is used for the thrust bearing design if a thrust bearing is used to carry this load, or is used to check the proper interference between the rider ring (thrust collars) and the pinion shaft. For the main low speed bull gear, there are multiple gear forces and thrust loads from multiple pinions. Following figure shows gear force and thrust force from one pinion. These forces have the same magnitude with opposite directions from previous pinion forces. Also, a thrust bearing must be used in the bull gear to carry the thrust load. To calculate the bull gear bearing reaction forces, the equations are the same as before, except we need to sum all the gear forces and thrust forces from each pinion also the addition of the thrust reaction force Rz from the thrust bearing.
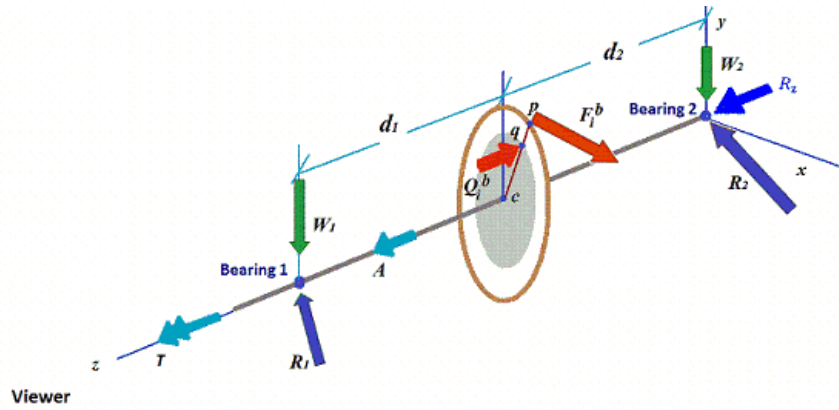
Steps are summarized below:

1. Reverse the gear force and thrust force from each pinion $F_i^b = -F$, $Q_i^b = -Q$. Note that if thrust bearings are used in the pinions, then $Q_i^b = 0$. The subscript b will be dropped in the following equations.

2. Pitch radius is the bull gear pitch radius Rp, the thrust contact point is $R_q = R_p + r_p - r_q$ if the thrust force is transmitted to the bull gear through rider ring

3. The displacement vectors for the gear force and thrust force will be in the positive radial direction, opposite to the pinion. That is $(\hat{e}_r)$ to replace $(-\hat{e}_r)$ in the above equations for the displacement vectors.

4. The applied axial force A now can be any axial force applied at the bull gear instead of aero load in the pinion. The axial force is balance with the reaction force from the thrust bearing R_z.

5. Again, force and moment balanced with the following equations:

$$\sum F_z = 0 \Rightarrow R_z = -\sum F_z - \sum Q_z - A_z$$

$$\sum M_y = 0 \Rightarrow R_{1x} = \frac{-1}{L}\sum(d_2 F_x - R_p \cos\theta F_z - R_q \cos\theta Q_z) \sum M_x = 0 \Rightarrow R_{1y} = \frac{-1}{L}\sum(-R_p \sin\theta F_z + d_2 F_y - R_q \sin\theta Q_z) + W_1$$

$$\sum F_x = 0 \Rightarrow R_{2x} = -R_{1x} - \sum F_x$$

$$\sum F_y = 0 \Rightarrow R_{2y} = -R_{1y} - \sum F_y + W_1 + W_2$$

Examples

This program calculates the bearing loads due to gear power transmission and aero thrust forces. No matter where the observer (viewer) stands, the coordinate system is defined as follows: The X-axis is to the right of the observer, Y-axis is to the top (opposite to the gravity direction), and Z-axis is towards to the observer, following the right-hand rule. The gravitational forces are in the negative Y (-Y) direction. Bearing #1 is the bearing close to the observer and bearing #2 is the bearing away from the observer. Following is a sketch shows that the observer is at the non-driver side, looking into the driver for a centrifugal compressor.

Z points to the observer
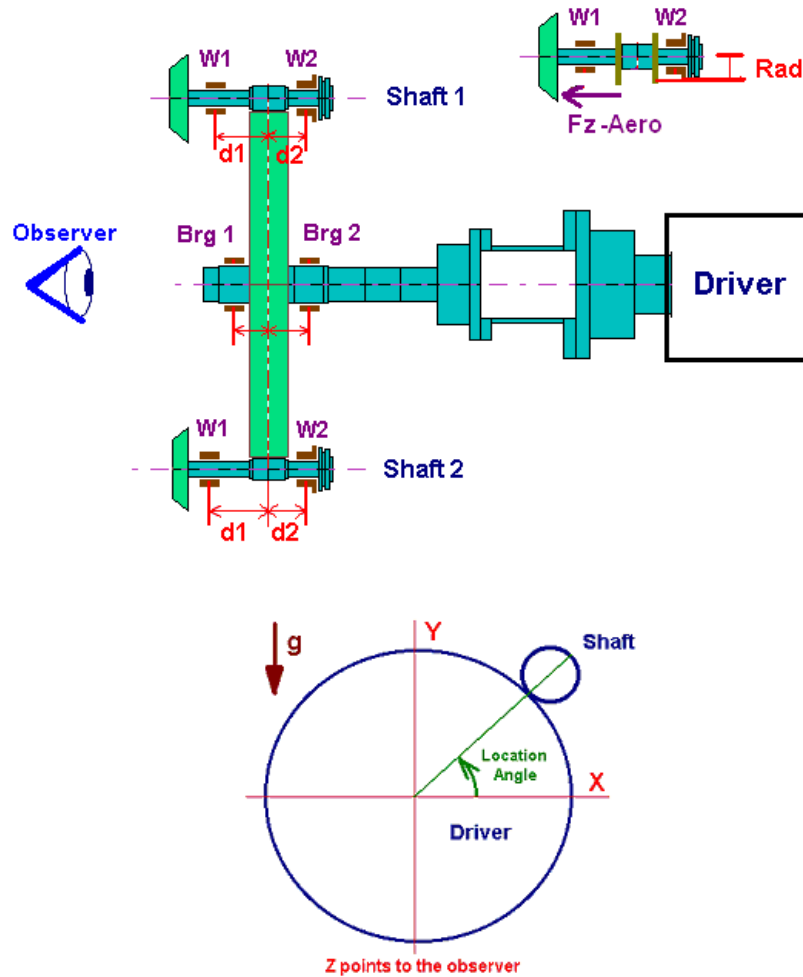
Example 1: Static loads only

The first example used here is a very simple example and only the static loads are considered. The horsepower is zero. Then the bearing forces are due to the static loads only. Draw a free-body diagram for the entire machine, the force and moment must be balanced. The summation of the radial bearing reaction forces and the gravity loads should be balanced. Since in this case, there is no thrust collar (rider ring) used to transmit the thrust to the low speed gear, the thrust load in the pinion is the aero load and the bull gear has no thrust load if no power transmission.
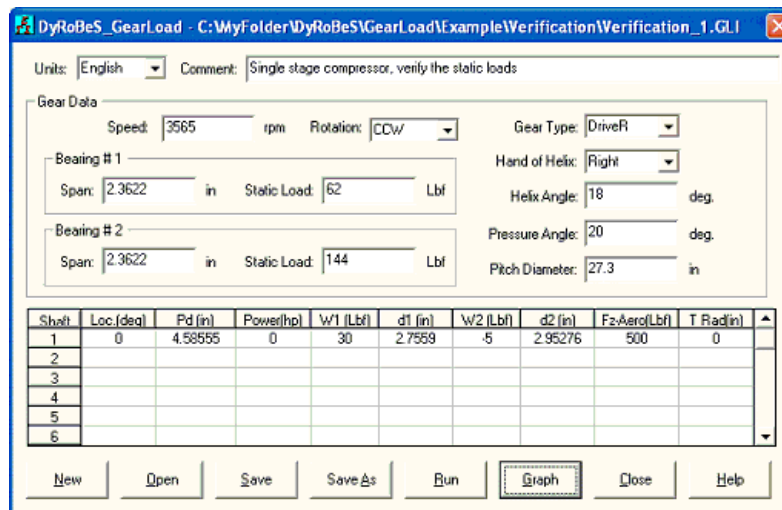
Fig 1-1
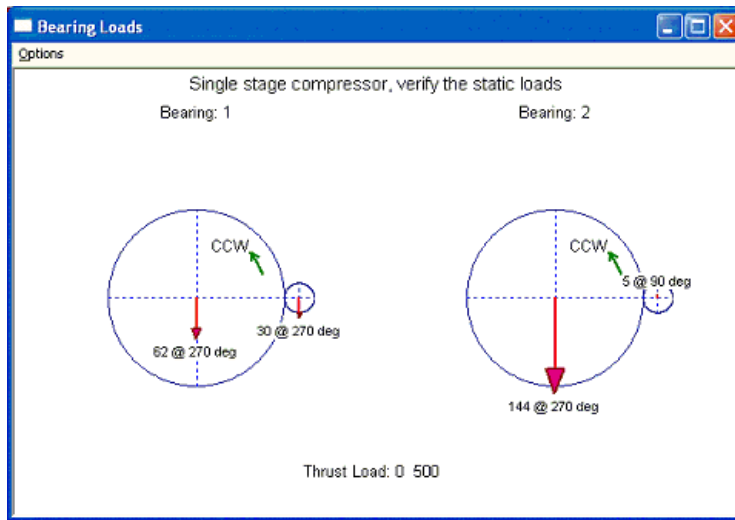
Fig 1-2

One may change the pinion location and static loads to verify the results. Following is the result for the pinion location at 145 degree. No matter where is the pinion located, the bearing loads are always equal to the static loads if power is zero in this example.
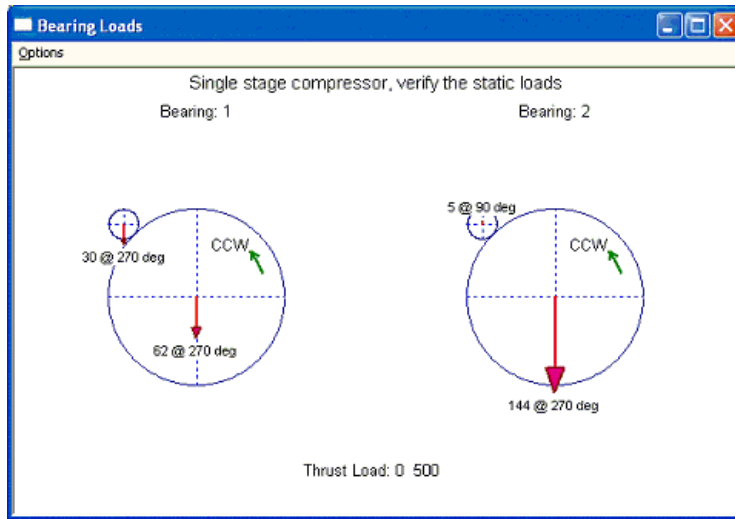
Fig 1-3

Example 2: Gear loads only, Spur gear

The second example is to neglect the static loads and only consider the gear loads. Input and output are shown below. Let us consider a spur gear (helix angle = 0) first which does not produce axial component of the gear force (thrust force), only the tangential (work) and radial (separation) forces exist. By neglecting the static loads, the only forces in the XY plane are the gear tangential and radial forces. With helix angle additional axial force is introduced. They are expressed as:

Ft = (60 * 6600 * HP) / (2*pi*RPM*Rp)

Fr = Ft * tan(pressure angle) / cos(helix angle)

Fa = Ft tan(helix angle)

Details of the equations are presented in the theoretical manual and not repeated here. In this case, HP = 265 HP, RPM = 3565 for the bull gear and 21,224 rpm for the pinion. The pitch diameter for bull gear is 27.3 inches and for pinion is 4.58555 inches. Since this is a gear set, RPM * RP should be the same for gull gear and pinion (3565 * 27.3/2 = 21224 * 4.58555/2 = 48,662.25). Therefore, Ft = 343.22, Fr = 124.92, Fa = 0. To get the bearing reaction forces, we need to use the force and moment balance equations. Since pinion is located at zero degree location from the driver gear. Therefore gear forces acting on the pinion is Fx=Fr=124.92, Fy=Ft=343.22, Fz=0. The forces on the bearing 1 of the pinion are calculated to be:

F1x = (2.95276 X 124.92) / (2.95276+2.7559) = 64.6

F1y = (2.95275 X 343.22) / (2.95276+2.7559) = 177.5

The magnitude of the force will be 189 at 70 degree on bearing 1 of the pinion.

The forces on the bearing 2 of the pinion are:

F2x = Fx - F1x = 60.3

F2y = Fy – F2x = 165.7

The magnitude of the force will be 176 at 70 degree on bearing 2 of the pinion.

The gear force acting on the bull gear will be the opposite of the gear force acting on the pinion. So, the forces on the bearing 1 of the bull gear are:

F1x = (2.3622 X (-124.92)) / (2.3622+2.3622) = -62.5

F1y = (2.3622 X (-343.22)) / (2.3622+2.3622) = -171.6

The forces on bearing 2 are:

F2x = -124.92 – (-62.5) = -62.5

F2y = -343.22 – (-171.6) = - 171.6

Both have the same magnitude of 183 at 250 degree. Also, the sum of all the forces is balanced (189+176-183-183 = 0). The forces are acting along the pressure line for spur gears without helix angle in this example, as illustrated in the tangential and radial forces equations. Note that bull gear is the driver gear in this example. For the bull gear bearings since the bearing span is identical, the loads are identical too for the balance of the moment. For pinion, the bearing 1 has a smaller bearing span (2.7559) than that of bearing 2 (2.95276). Therefore, the load on bearing 1 (189) is larger than that of bearing 2 (176). Again, there is no axial gear force due to zero helix angle and the thrust load on the pinion is the aero load and bull gear has zero thrust load.
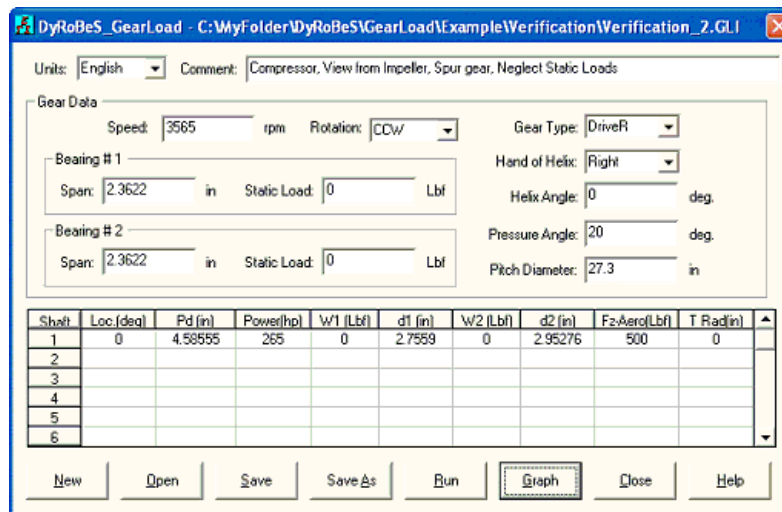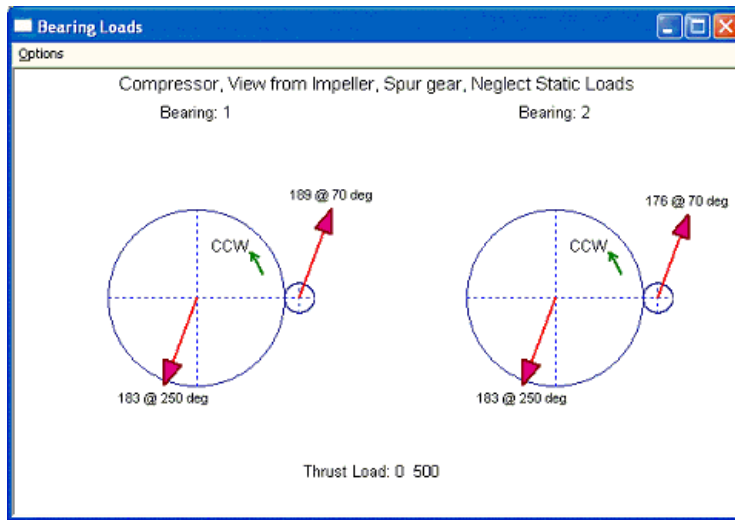

Fig 2-1

Fig 2-2

Let us change the pressure angle to be 15 degree. The result is shown below. Again the forces are along the pressure line and the bull gear is the driver gear in this example. Also, the forces on the bearings are different from previous case due to different radial gear forces from different pressure angle. However, the force and moment are still balanced.
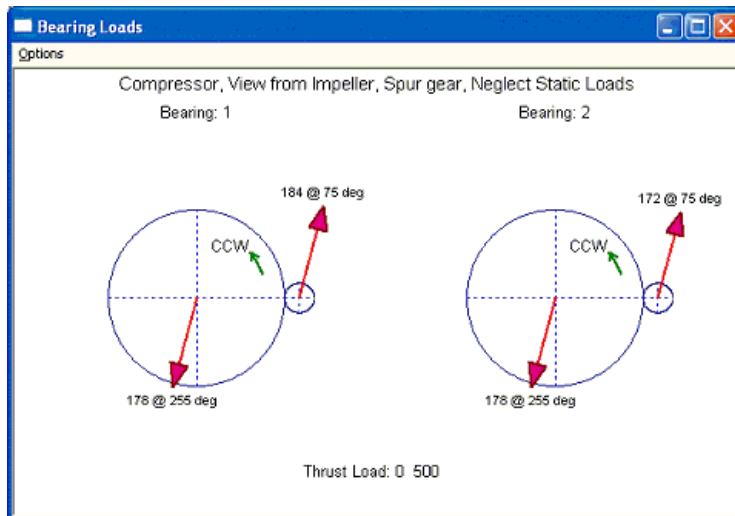

Fig 2-3

Next, let us change the driver unit and make the low speed gear as a driven unit and high speed pinion as the driver. Now, the forces are still acting along the pressure line, but pinion is the driver unit and bull gear is the driven unit. The magnitudes of the forces are still the same, but directions are different from case 1.
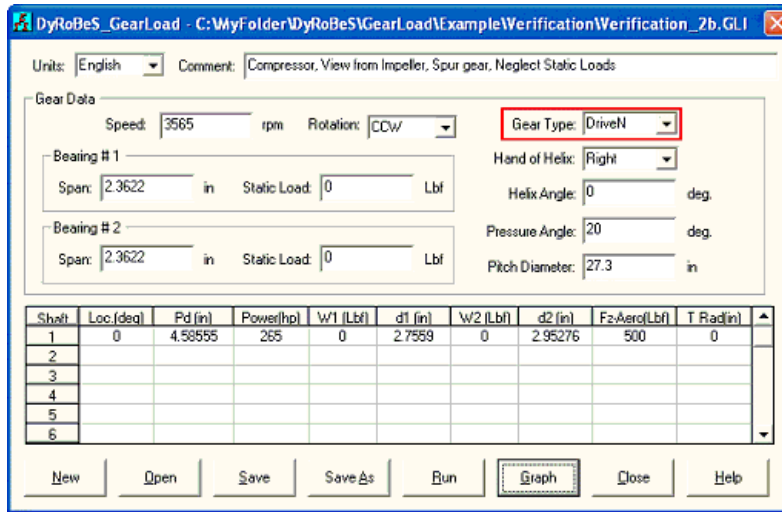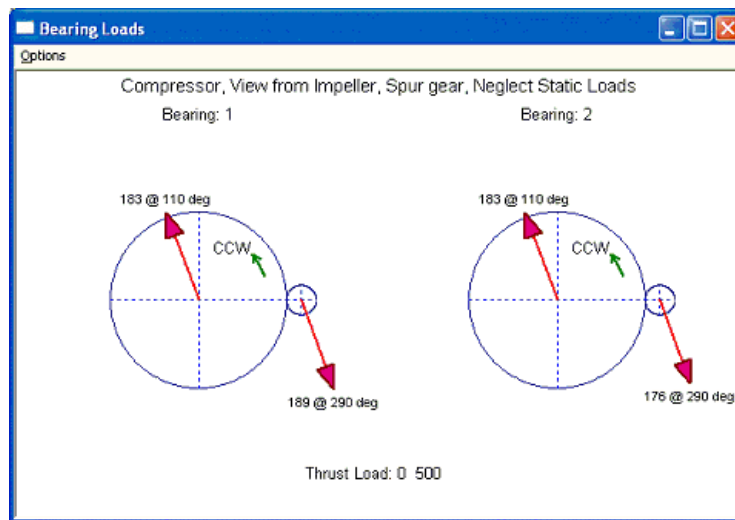
Fig 2-4

Fig 2-5

Following this case, let us move the driver pinion to be on top of the driven gear, that is, the driving pinion is located 90 degree right on top of the driven low speed bull gear. The result is shown below. Again, the forces are along the pressure line and force and moment are balanced.
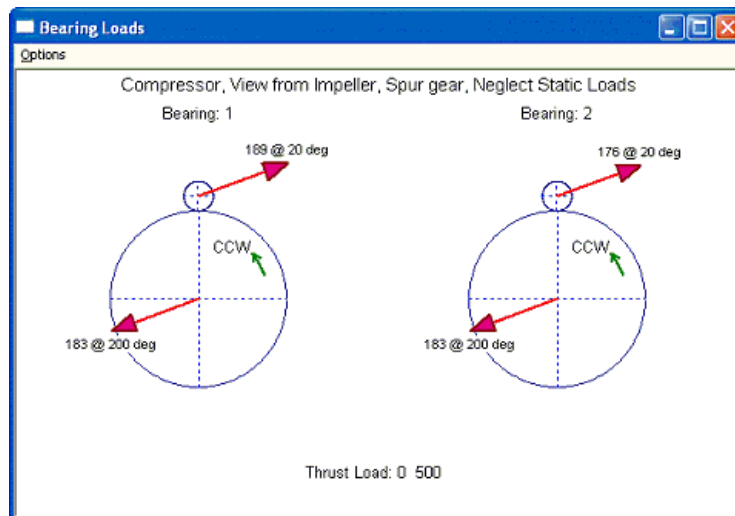

Fig 2-6

Next, let us move the driving pinion back to the zero degree and change the direction of rotation of the driven gear to be CW. The results are identical to Fig. 2.2. That is if the low speed gear is a driver unit and rotates CCW has the same force vector as if the low speed gear is a driven unit and rotates CW.
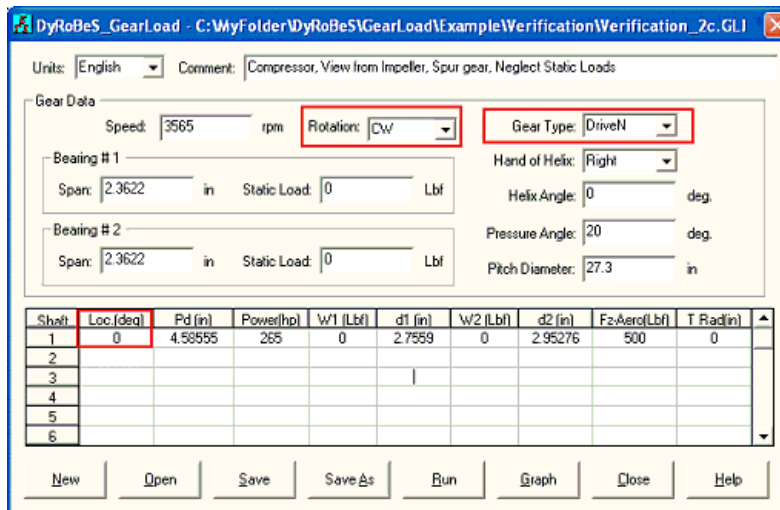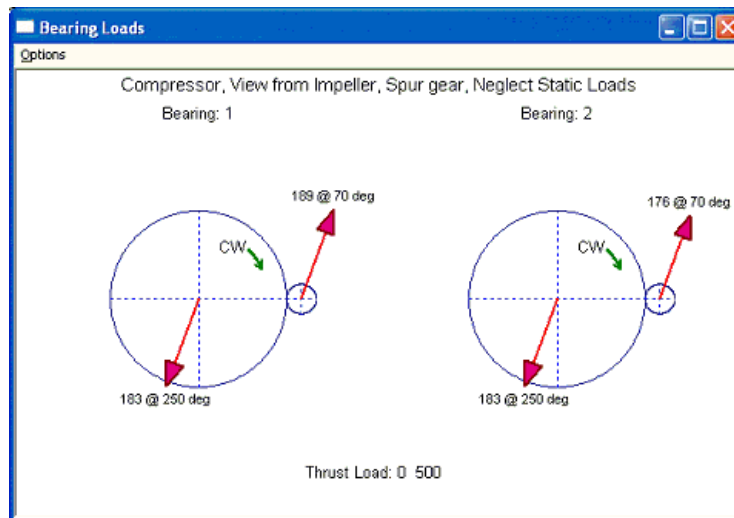

Fig 2-7

Fig 2-8

Example 3: Gear loads only, Helical gear

Use the example in example 2 case 1 and add the helix angle of 18 degrees. When the low speed gear is the driver and rotates CCW with right hand of helix, viewed from the axis of rotation, the axial component of the gear force acting on the pinion is in the negative Z direction (away from the observer) and opposite to the aero thrust load. Therefore, the thrust load at the pinion is the aero load minus the gear axial load (500 – 112 = 388) and this load must be carried by a thrust bearing on the pinion. With the action and reaction relationship, the thrust load at the driver (bull gear) will be the axial gear load of 112 which will be carried by a thrust bearing at the bull gear shaft. However, this gear axial load is acting on the pitch diameter, it produces a large moment acting on the bearing. The moment can be high if the gear pitch diameter is large. Consider the bull gear shaft, the axial load is 112 and the pitch diameter is 27.3, the moment in the (-Y) direction acting on the bearing will be (112X(27.3/2) = 1529). The magnitude of the force acting on the bearing will be the moment divides the bearing span. For bull gear bearings, the total bearing span is (2.3622X2=4.7244), the force will be (1529/4.7244=324). Since this axial force is positive acting on the bull gear, the additional force due to this moment acting on the bull gear bearing 1 will be 324 in the 180 degree direction (-X) and 0 degree (+X) direction on the bearing 2. This effect can be seen by comparing the force diagram with the helix angle = 0 in previous example (Example 2 – case 1). For the driven pinion the pitch diameter is small, the moment due to axial load is also small. Also, with the introduction of helix angle, the gear radial force component also changes slightly. A sketch illustrating this axial gear load effect is shown below.
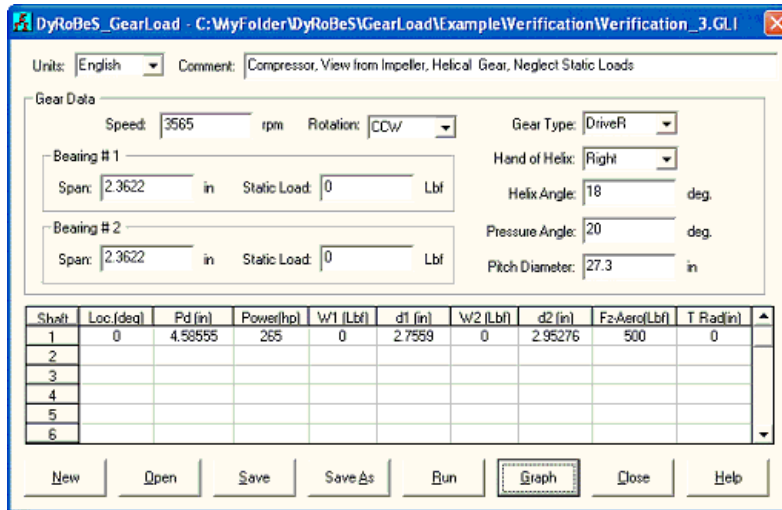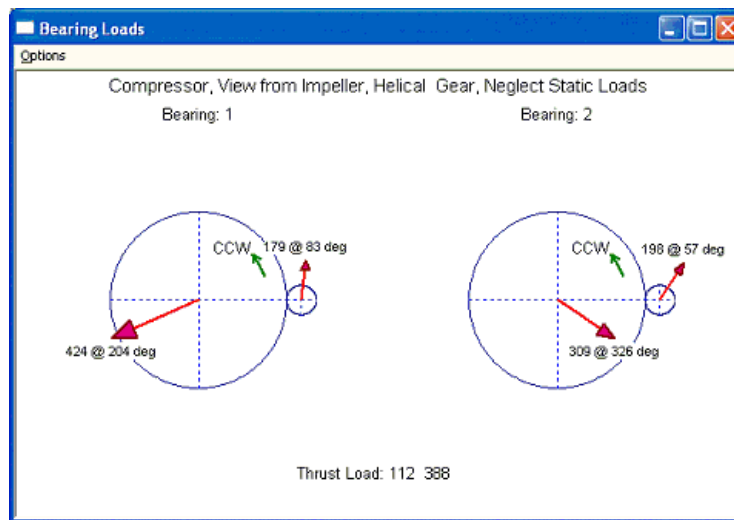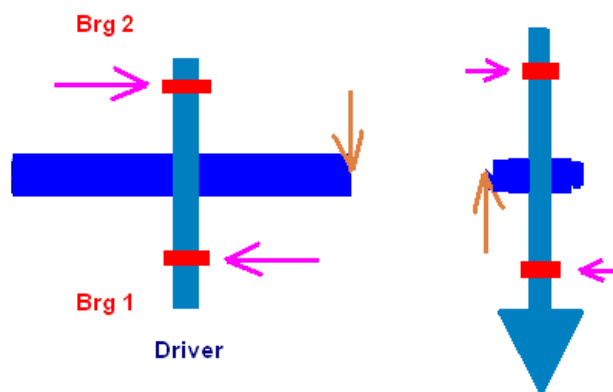
Fig 3-1

Fig 3-2

Fig 3-3

Example 4: Gear loads + Static loads, Helical gear

In the example, let us add the static loads on the bearings back. Now, the total bearing loads will be the sum of the gear forces and the static loads.
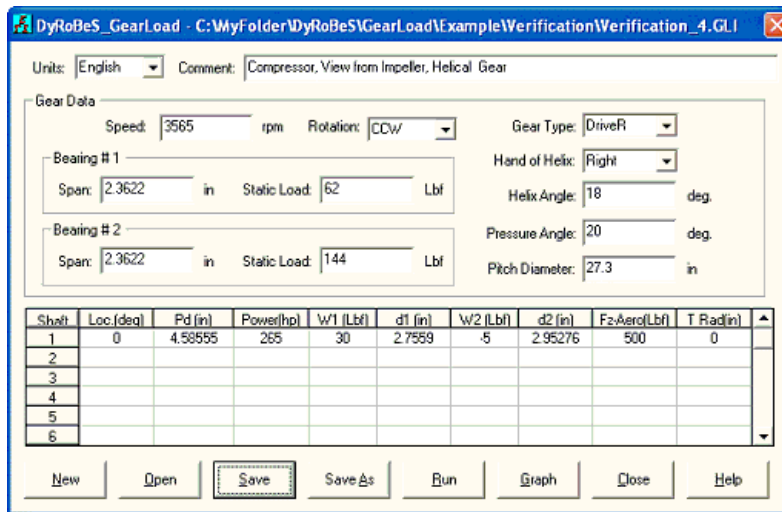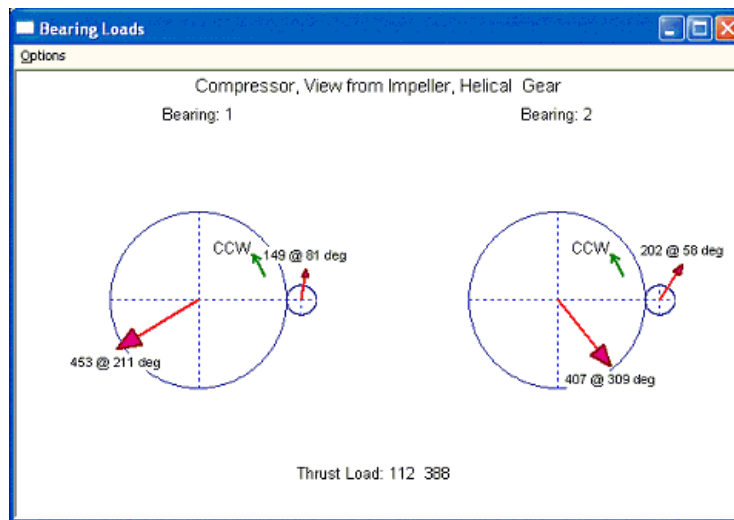
Fig 4-1

Fig 4-2

Let us check the bearing 1 on bull gear. Without the static load, the load is 424 at 204 degree, as illustrated in Example 3. With the static load 62 at 270 degree, the vector sum becomes 453 at 211 degree. For bearing 2 on the pinion, without the static load, the load is 198 at 57 degree. With the static load 5 at 90 degree, the total bearing load becomes 202 at 58 degree. Same discussions are applied for other 2 bearings.

Example 5: Expander Application

Let us consider the low speed gear is a driven unit and high speed pinion is a driver unit, such as in the expander applications. First, let us consider the helix angle is zero such that the axial gear force can be eliminated and only the gear radial and tangential forces are considered with the bearing static loads. Comparing Fig. 5.2 to the Fig. 2.5, noticed that the resulting bearing load vector of Fig 5.2 has shifted towards the bearing static load. Actually, the sum of the load vectors in Fig. 2.5 and the static loads will result in the Fig. 5.2. For example, the load vector for bearing 2 of the bull gear without static load is 183 at 110 degree. The static load is given as 144 at 270 degree. The resulting vector will be the vector summation and is 68 at 156 degree. Others can be verified in the same way.
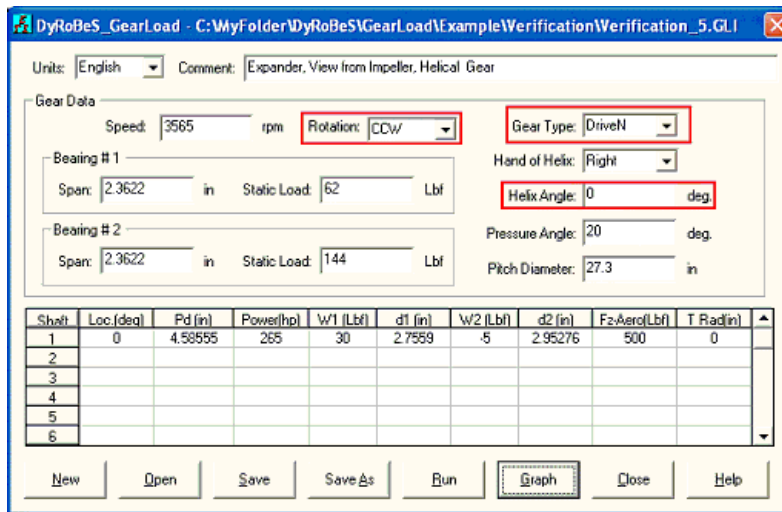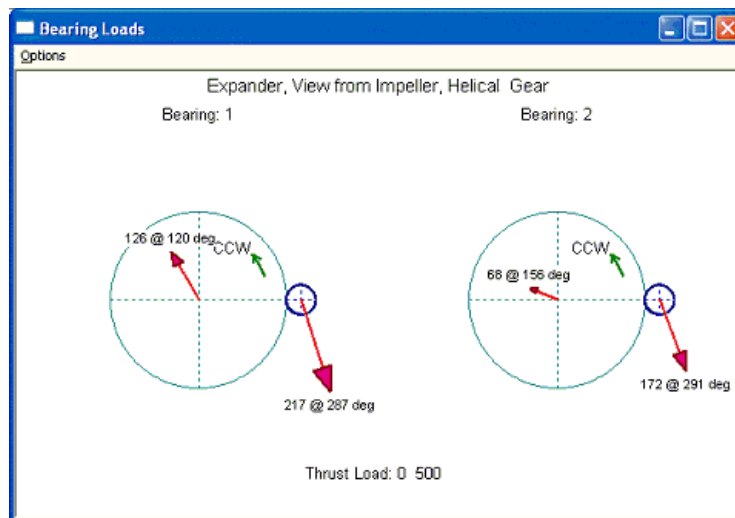
Fig 5-1

Fig 5-2

Now, let us put back the helix angle. The input and output are shown below. The results are significantly different from previous discussion without helix angle. With the introduction of the helix angle, it creates an axial gear force. The gear force in this configuration is toward the viewer (positive Z direction) for the high speed pinion and away from the viewer (negative Z direction) for the low speed gear. Because of the positive thrust load at the pinion, the total thrust load becomes the sum of the aero load and the gear axial force, not the difference as example 4. This is significant for the high speed pinion thrust bearing design since the thrust load is 612 instead of 388 as previous example. The bearing radial loads are also changed due to this reversal of the gear axial load and the associated moment, as explained before and sketched below. Again, this effect is significant in the bull gear bearing load due to large moment arm (pitch radius) and small in the pinion due to smaller moment arm.

Fig 5-3
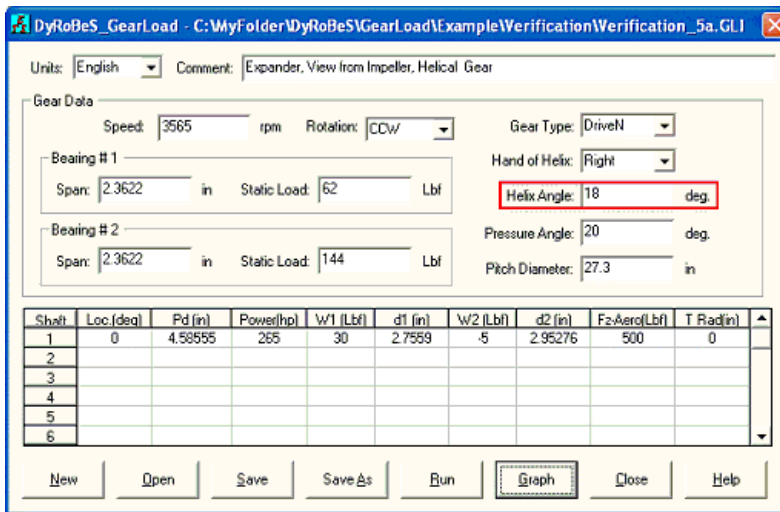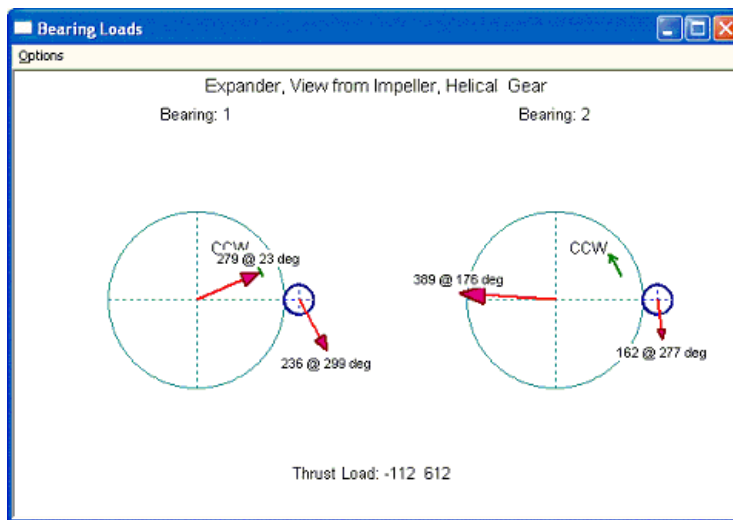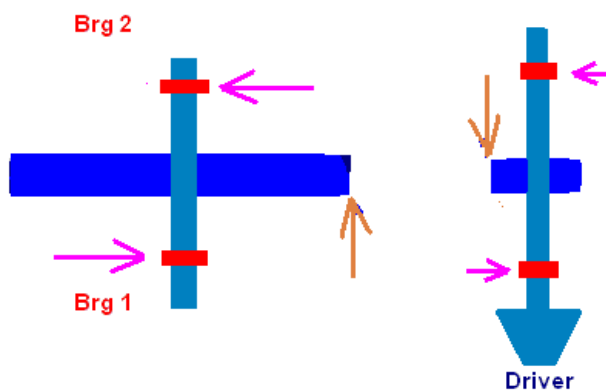

Fig 5-4

Fig 5-5

In order to reduce this thrust load at the high speed pinion, let us change the rotation of direction of the low speed bull gear to be CW. The input and output are shown below. No surprise, that the results are now identical to the Fig 4.2. That is if both the direction of rotation and driver/driven role change, then the results are identical due to the same gear force.
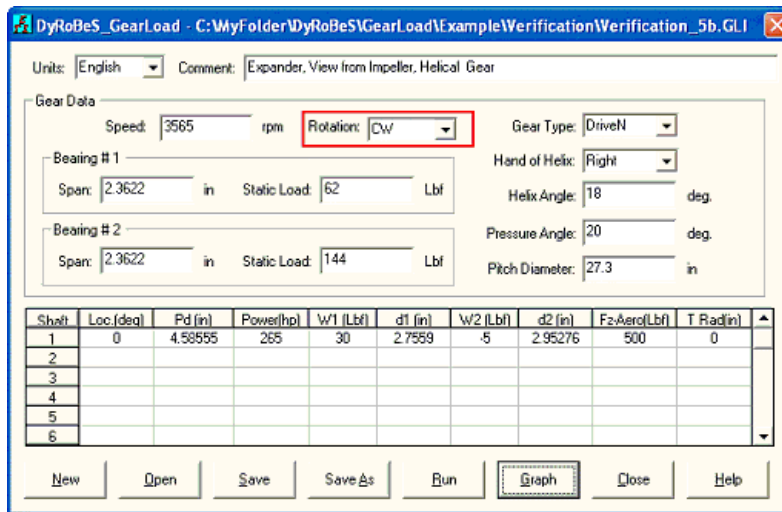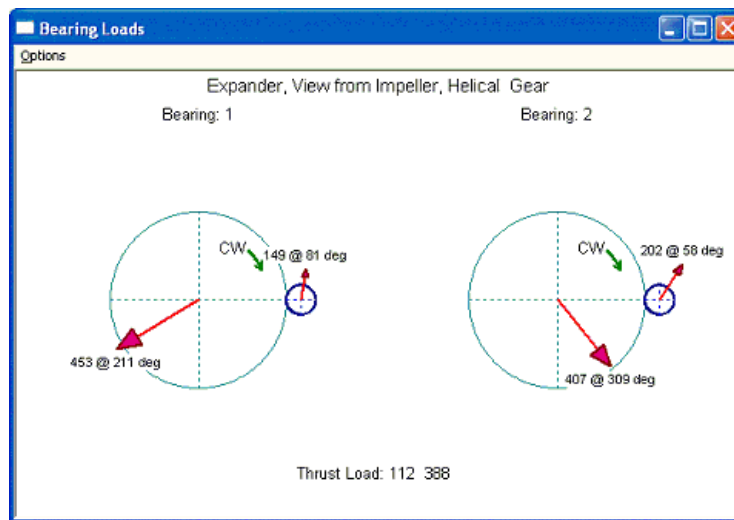
Fig 5-6

Fig 5-7

Example 6: Single stage compressor and expander application

Very often in the integrally geared compressors, blowers, pumps, turbines, and expanders, the speed of the high speed pinion is very high, which results in high mechanical loss. Therefore, it is common to have so called thrust collar (or rider ring) at both ends of the pinion to transfer the thrust load from the high speed pinion to the low speed bull gear through the gears. This will eliminate the thrust bearing in the pinion. However, it will introduce an additional axial load on the thrust collar and its effect can be significant in the low speed bull gear bearing load due to the large moment arm (pitch radius).

Case 1- Compressor Application

Input and output of this example are shown below. With the introduction of the rider ring, the high speed compressor aero thrust load is transferred to the low speed bull gear thrust bearing. The gear axial force on the pinion is 112 away from the viewer (-Z direction) and the aero force is 500 toward viewer (+Z direction). The resulting net force (500-112=388) is acting on the bull gear toward the viewer. It is very similar with Fig. 3.3, however, this resulting net force is acting on the rider ring with moment arm equal pitch radius of bull gear + pitch radius of pinion – rider ring radius ((27.3/2)+(4.58555/2)-2.45=13.49278). The force couple to form this moment on the bull gear bearings is 388X13.49278/(2.3622X2) = 1108.119. For bearing 1 of the bull gear, this force is toward the (-X) direction and for bearing 2 of the bull gear, this force is toward the (+X) direction in this configuration. For bearing 1 of the bull gear, without the rider ring, the force vector is 453 @ 211 degree (from Fig 4.2), for bearing 2 is 407 @ 309 degree. With this additional force from the rider ring, the resulting forces for bull gear bearings are: 1515 @ 189 degree for bearing 1 and 1402 @ 347 degree.
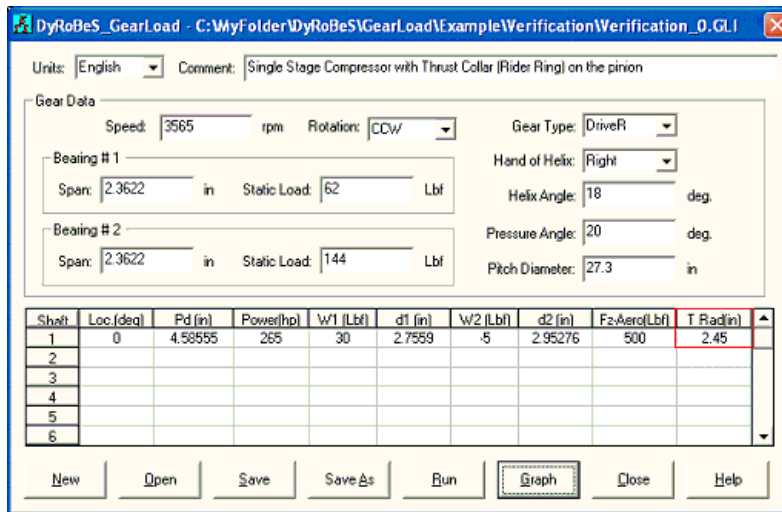
Fig 6-1
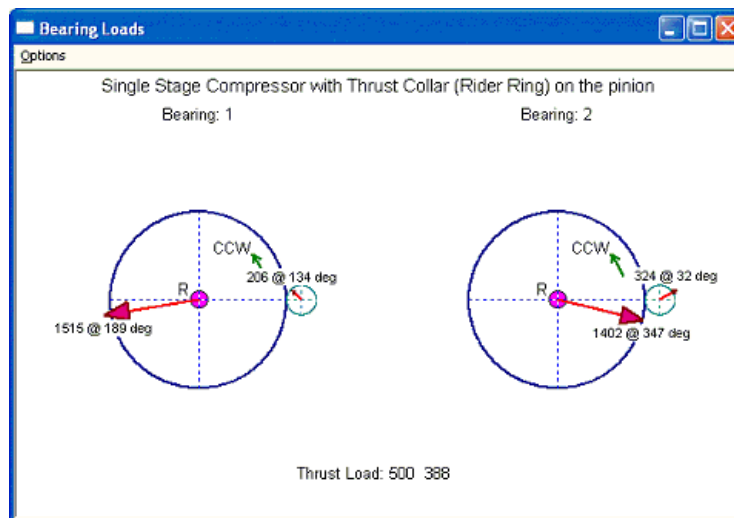
Fig 6-2

Since there is only one pinion in the system, let us switch the gear and consider the pinion is the reference gear, The inputs are shown below. Note that the direction of rotation, gear type, and hand of helix have changed from CCW to CW, DriveR to DriveN, and Right to Left. The angular position of the bull gear is now at 180 degree relative to the reference shaft (pinion now). The thrust force now is a NEGATIVE value. It is because the original thrust load is 500 Lb force transmitted from the pinion and acting on the bull gear bearing. However, since this input is the load acting on the rotor, so it has to become negative value in indicate that this force is acting on the rotor. Also, the radius of action is now Rp+rp-Trad (pitch radius of bull gear + pitch radius of pinion – thrust radius). As expected, the results are identical to the previous case.
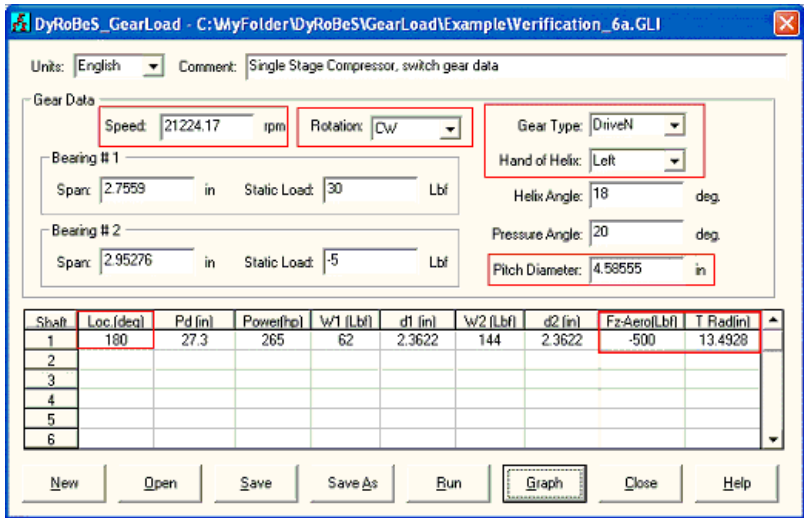
Fig 6-3
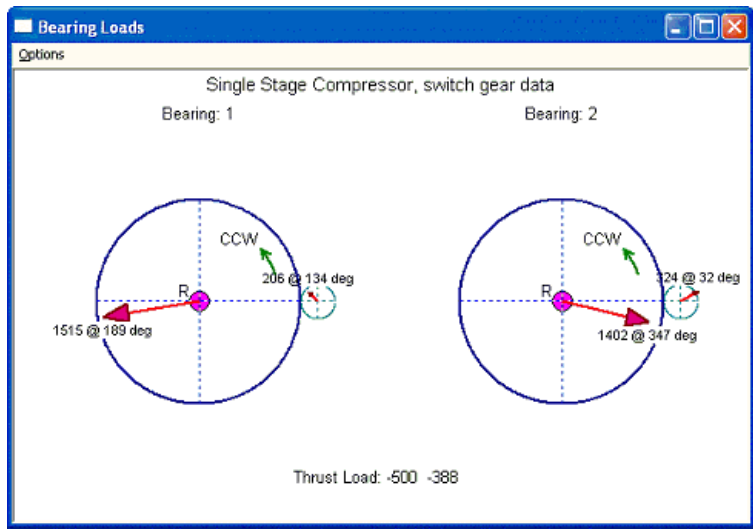
Fig 6-4

Case 2- Expander Application

Use this example again, however now the pinion is the driver and the bull gear becomes a driven unit. All other data are the same as before. First let us use bull gear as the reference shaft, and inputs and outputs are shown below. Note that, in this case, the gear axial force is in the same direction as the aero force, therefore, the pinion net thrust load is the sum of gear axial force and the aero force.
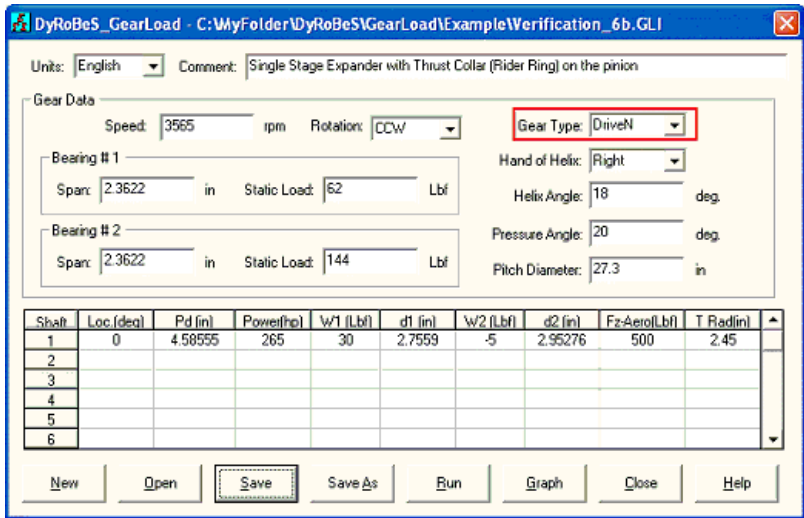
Fig 6-5
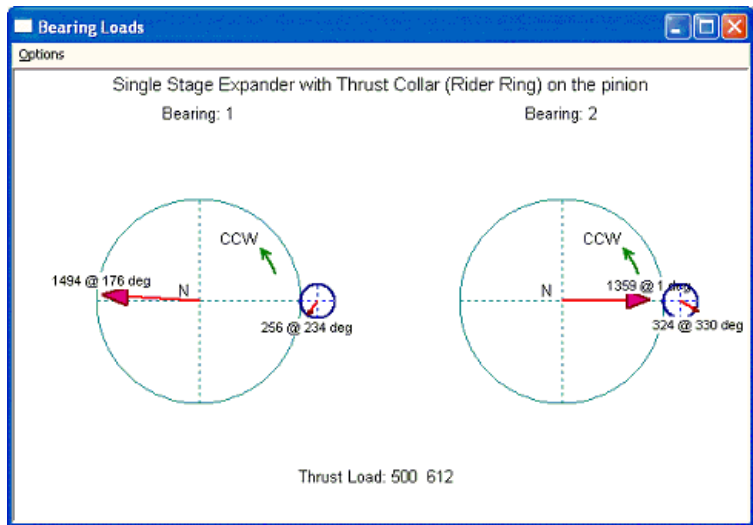
Fig 6-6
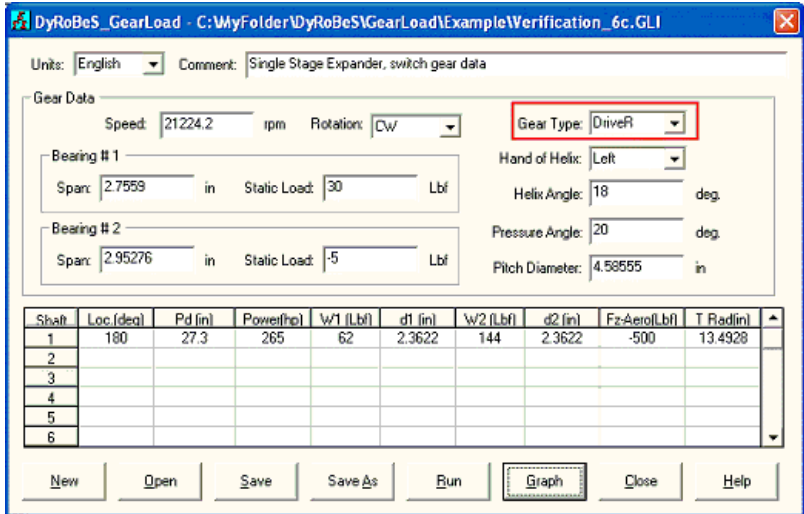
Fig 6-7
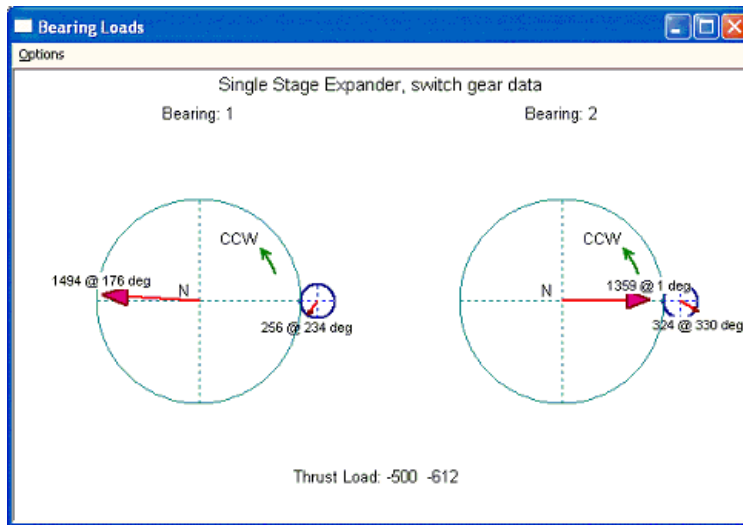
Fig 6-8

Example 7: A single stage blower with thrust bearing or thrust ring on the pinion

Case1: A single stage compressor or blower is used in this example. A motor drives a bull gear and the bull gear drives a high-speed pinion which carries an impeller. Impeller compresses air. For the high-speed pinion, a thrust bearing is used to carry the thrust load acting on the pinion. Therefore, there is no need to enter the aero thrust load for radial bearing load analysis. The viewer is in front of the impeller and looking into the driver (motor in this case). Bearing #1 will be the bearing in the air side and bearing #2 will be the bearing near the motor side. The Input screen and outputs (graph and text) are shown below:

Fig 7-1

Fig 7-2

Text Outputs:

```
***** Coordinate System *****
 X-Axis to the right,  Y-Axis to the top,  Z-axis to the Observer
 Gravitational forces applied in the -Y direction
 Angle measured CCW from the +X Axis (Right Hand Rule)

 Brg#1 is the brg closest to the observer
 Brg#2 is the brg farest to the observer

***** System Description *****
 Single stage compressor (blower), viewed from non-driver side

***** Reference Shaft Data *****
 Rotational Speed (rpm):    3565.00
 Gear Number...........:       1
 Driver/Driven Gear....:    DRIVER
 Hand of Helix.........:     RIGHT
 Direction of Rotation.:     CCW
 Helix Angle.....(Degs):    18.0000
 Pressure Angle..(Degs):    20.0000
 Pitch Diameter....(in):    27.30000
 Brg#1 Span/gear...(in):    2.36220
 Brg#2 Span/gear...(in):    2.36220

***** Bearing Loads Calculation *****
                        <Reference>....<<Shafts.......---->
 Shaft #...................:              1
 Reference Shaft Gear#.....:              1
 Angular Location....(Degs):                  .00
 Rotational Speed.....(rpm):    3565.00   21224.17
 Pitch Diameter........(in):               4.58555
 HorsePower...........(hp):     265.00     265.00
 Gear Force Components (Lbf)
 Acting on the driven shafts
 Tangential (Work) force...:               343.22
 Radial (Separating) force.:               131.35
 Axial (Thrust) force......:              -111.52
 External Load (Aero Load)
       Axial Aero Load (Lbf):                  .00
       Thrust At Radius (in):               .00000

 Brg#1 Static Load....(Lbf):    62.0000    30.0000
       Span/Gear tooth.(in):               2.7559
       Load (X-dir)...(Lbf): -387.8788    23.1504
       Load (Y-dir)...(Lbf): -233.6086   147.5264
       Load (mag.)....(Lbf):  452.7946   149.3318
       Load (angle)..(Degs):   211.06     81.08

 Brg#2 Static Load....(Lbf):   144.0000    -5.0000
       Span/Gear tooth.(in):               2.9528
       Load (X-dir)...(Lbf):  256.5293   108.1991
       Load (Y-dir)...(Lbf): -315.6086   170.6908
       Load (mag.)....(Lbf):  406.7137   202.0950
       Load (angle)..(Degs):   309.10     57.63
```

```
     Thrust Brg Loads.....(Lbf):   111.5180  -111.5180
 ***** End of Analysis *****
```

Case 2: Now, let us view the machine from the driver (motor) side. The direction of rotation is reversed from previous input. Also, the X and Z coordinates are reversed. The bearing #1 is now the bearing at the driver (motor) side and bearing #2 is the bearing away from the driver since the observer is in the driver side now. The shaft angular position is also flipped horizontally from zero to 180 deg. The input and outputs are shown below. Note that since the Z axis is reversed, the thrust loads are now also reversed.
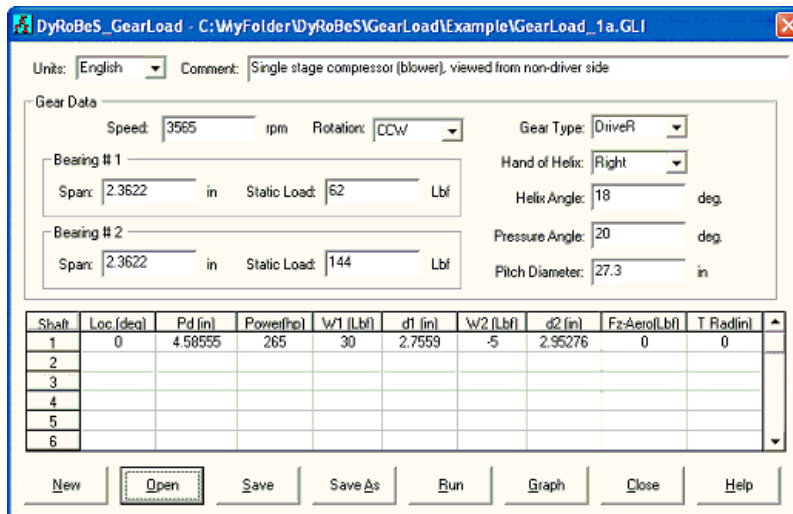

Fig 7-3
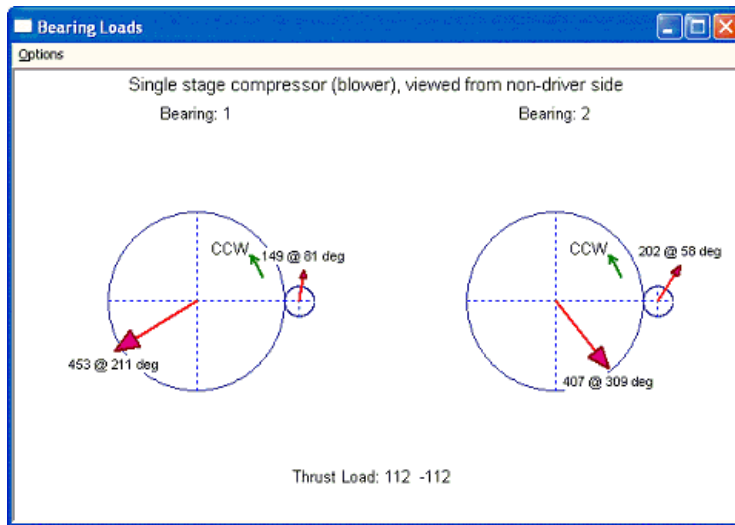

Fig 7-4

```
***** Coordinate System *****
 X-Axis to the right,  Y-Axis to the top,  Z-axis to the Observer
 Gravitational forces applied in the -Y direction
 Angle measured CCW from the +X Axis (Right Hand Rule)

 Brg#1 is the brg closest to the observer
 Brg#2 is the brg farest to the observer

***** System Description *****
 Single stage compressor (blower), viewed from driver side

***** Reference Shaft Data *****
 Rotational Speed (rpm):   3565.00
 Gear Number...........:      1
 Driver/Driven Gear....:    DRIVER
 Hand of Helix.........:    RIGHT
 Direction of Rotation.:    CW
 Helix Angle.....(Degs):   18.0000
 Pressure Angle..(Degs):   20.0000
```

```
   Pitch Diameter....(in):  27.30000
   Brg#1 Span/gear...(in):   2.36220
   Brg#2 Span/gear...(in):   2.36220

 ***** Bearing Loads Calculation *****
                          <Reference>....<<Shafts.......---->
   Shaft #...................:              1
   Reference Shaft Gear#.....:              1
   Angular Location....(Degs):         180.00
   Rotational Speed.....(rpm):   3565.00  21224.17
   Pitch Diameter........(in):          4.58555
   HorsePower...........(hp):    265.00    265.00
   Gear Force Components (Lbf)
   Acting on the driven shafts
   Tangential (Work) force...:          343.22
   Radial (Separating) force.:          131.35
   Axial (Thrust) force......:         -111.52
   External Load (Aero Load)
        Axial Aero Load (Lbf):             .00
        Thrust At Radius (in):          .00000

   Brg#1 Static Load....(Lbf):   144.0000   -5.0000
         Span/Gear tooth.(in):             2.9528
         Load (X-dir)...(Lbf): -256.5293 -108.1991
         Load (Y-dir)...(Lbf): -315.6086  170.6908
         Load (mag.)....(Lbf):  406.7137  202.0950
         Load (angle)..(Degs):    230.90    122.37

   Brg#2 Static Load....(Lbf):    62.0000   30.0000
         Span/Gear tooth.(in):             2.7559
         Load (X-dir)...(Lbf):  387.8788  -23.1504
         Load (Y-dir)...(Lbf): -233.6086  147.5264
         Load (mag.)....(Lbf):  452.7946  149.3318
         Load (angle)..(Degs):    328.94     98.92

   Thrust Brg Loads.....(Lbf): -111.5180  111.5180
 ***** End of Analysis *****
```

In the Ver 3.0, the graph can be viewed from the opposite side. For example, in this above case, although our analysis was performed as viewer in the driver side, the bearing loads can be graphed from the opposite side, that is viewed from the air side as the first case.
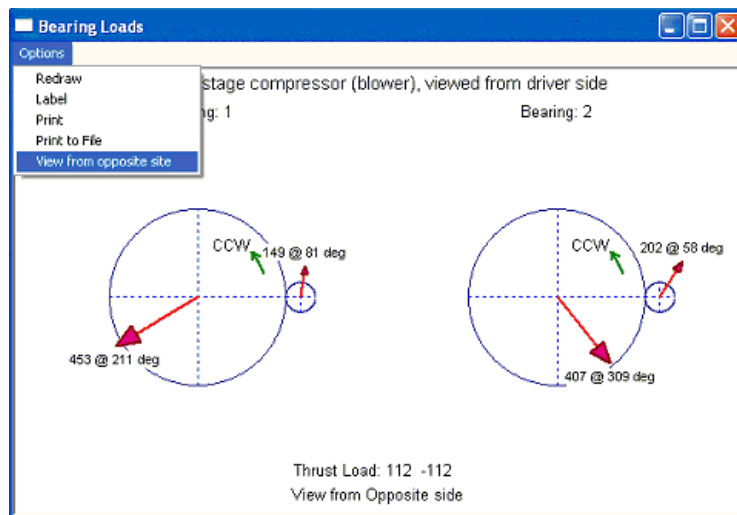
Fig 7-5

This also illustrates that no matter where the observer (viewer) is, the bearing loads are identical. Since in the above cases, the aero thrust load was not supplied in the input, the thrust loads due to helical gear force on low-speed bull gear and high-speed pinion are identical in magnitude and opposite in sign. Without helical angle, the axial gear force will be null.

Case 3: Now, let us add aero thrust load on the pinion as shown below. A thrust bearing is used in the pinion to carry the thrust load. Therefore, the thrust load from high speed pinion is not transmitted to the low speed bull gear. The thrust collar radius is entered as zero for thrust bearing application. The results show that the radial bearing loads and associated angles are not affected by this aero thrust load if a thrust bearing is used in the high speed pinion. As expected, the only difference is the thrust load on the high-speed pinion. The resulting thrust load on the pinion is the sum of aero load and gear axial force that a thrust bearing must be abale to carry this net thrust load. The thrust load on the gull gear is the same as before.
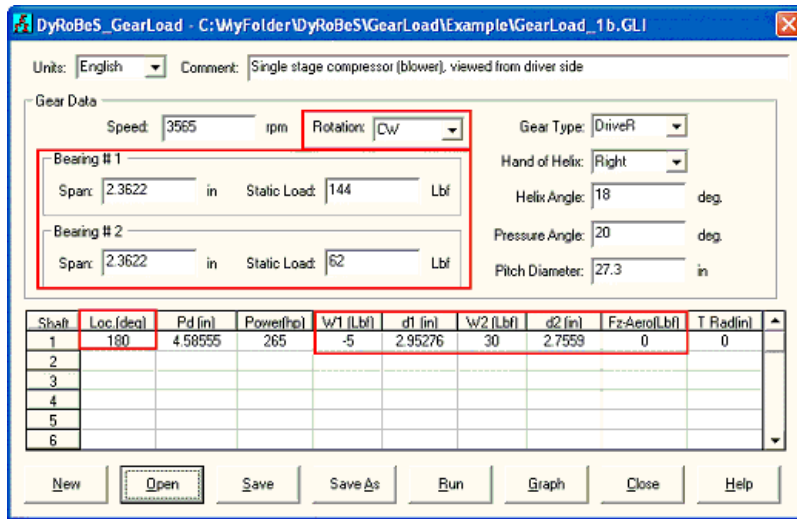
Fig 7-6
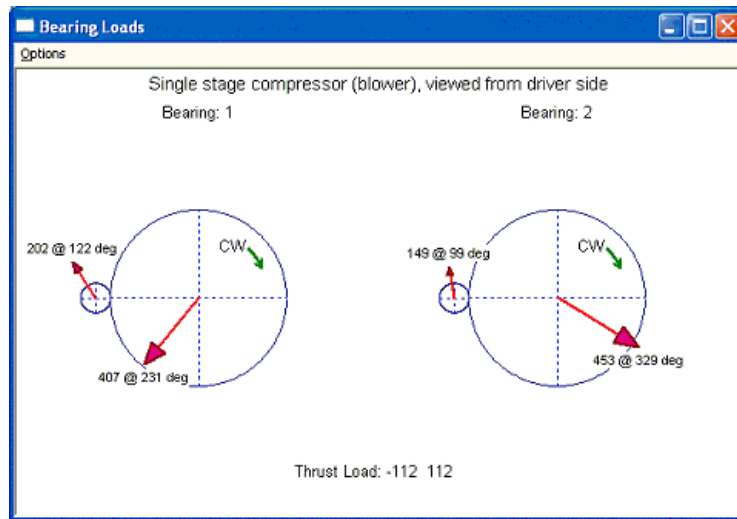

Fig 7-7

```
***** Coordinate System *****
 X-Axis to the right,  Y-Axis to the top,  Z-axis to the Observer
 Gravitational forces applied in the -Y direction
 Angle measured CCW from the +X Axis (Right Hand Rule)

 Brg#1 is the brg closest to the observer
 Brg#2 is the brg farest to the observer

***** System Description *****
 Single stage compressor (blower), viewed from non-driver side

***** Reference Shaft Data *****
 Rotational Speed (rpm):    3565.00
 Gear Number...........:       1
 Driver/Driven Gear....:    DRIVER
 Hand of Helix.........:    RIGHT
 Direction of Rotation.:    CCW
 Helix Angle.....(Degs):   18.0000
 Pressure Angle..(Degs):   20.0000
 Pitch Diameter....(in):   27.30000
 Brg#1 Span/gear...(in):    2.36220
 Brg#2 Span/gear...(in):    2.36220

***** Bearing Loads Calculation *****
                      <Reference>....<<Shafts.......---->
 Shaft #...................:              1
 Reference Shaft Gear#.....:              1
 Angular Location....(Degs):             .00
 Rotational Speed.....(rpm):   3565.00   21224.17
 Pitch Diameter........(in):             4.58555
```

```
HorsePower............(hp):      265.00      265.00
Gear Force Components (Lbf)
Tangential (Work) force...:                  343.22
Radial (Separating) force.:                  131.35
Axial (Thrust) force......:                 -111.52
External Load (Aero Load)
      Axial Aero Load (Lbf):                 500.00
      Thrust At Radius (in):                 .00000

Brg#1 Static Load....(Lbf):      62.0000     30.0000
      Span/Gear tooth.(in):                   2.7559
      Load (X-dir)...(Lbf):   -387.8788      23.1504
      Load (Y-dir)...(Lbf):   -233.6086     147.5264
      Load (mag.)....(Lbf):    452.7946     149.3318
      Load (angle)..(Degs):      211.06       81.08

Brg#2 Static Load....(Lbf):     144.0000     -5.0000
      Span/Gear tooth.(in):                   2.9528
      Load (X-dir)...(Lbf):    256.5293     108.1991
      Load (Y-dir)...(Lbf):   -315.6086     170.6908
      Load (mag.)....(Lbf):    406.7137     202.0950
      Load (angle)..(Degs):      309.10       57.63

Thrust Brg Loads.....(Lbf):     111.5180    388.4820
Force acting on the Thrust Brgs
Each rotor has its own thrust bearing
***** End of Analysis *****
```

Case 4: Let us consider using thrust collar (sometimes called Rider Ring) on the pinion which is utilized to transfer the thrust load from high-speed pinion to the low speed bull gear. This will eliminate the use of thrust bearing on the pinion and reduce the mechanical power loss caused by the high-velocity in the pinion bearing. Instead, a low-velocity thrust bearing on the bull gear will carry the load. The thrust collar (rider ring) on the pinion has a radius of 2.45 inches. The input and outputs are shown below. It shows that there are significant increases in the bearing loads due to the rider ring (thrust collar) design. This additional force is caused by the moment from the axial force acting on the thrust collar. This effect is significant when the pitch diameter or collar radius is large which yields large moment arm. The thrust load on the bull gear is now the aero load from the high speed pinion. The pinion thrust load is the thrust load from pinion acting on the rider ring. It is the sum of the aero load and the gear axial force. This is an internal force from pinion to the bull gear.
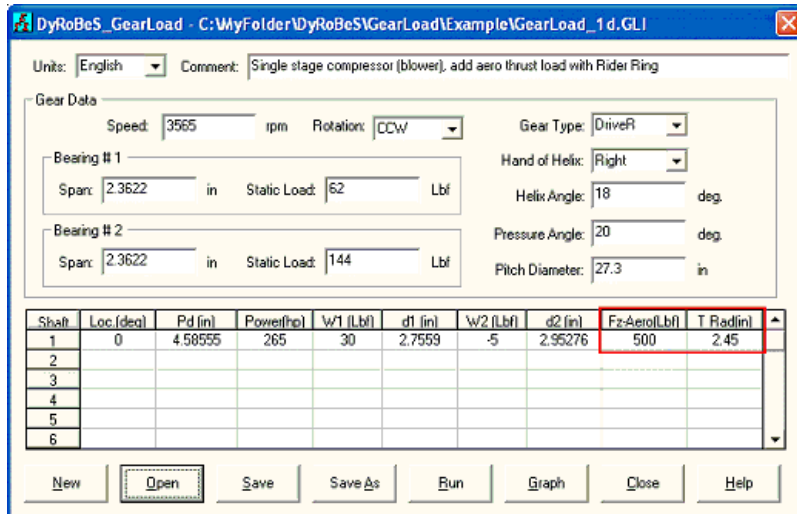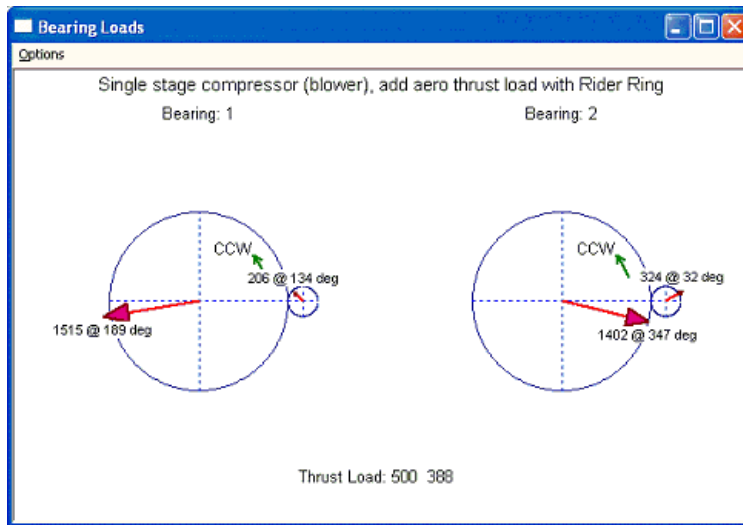

Fig 7-8

Fig 7-9

```
***** Coordinate System *****
 X-Axis to the right,  Y-Axis to the top,  Z-axis to the Observer
 Gravitational forces applied in the -Y direction
 Angle measured CCW from the +X Axis (Right Hand Rule)

 Brg#1 is the brg closest to the observer
 Brg#2 is the brg farest to the observer

***** System Description *****
 Single stage compressor (blower), add aero thrust load with Rider Ring

***** Reference Shaft Data *****
 Rotational Speed (rpm):    3565.00
 Gear Number...........:       1
 Driver/Driven Gear....:    DRIVER
 Hand of Helix.........:    RIGHT
 Direction of Rotation.:    CCW
 Helix Angle.....(Degs):   18.0000
 Pressure Angle..(Degs):   20.0000
 Pitch Diameter....(in):  27.30000
 Brg#1 Span/gear...(in):   2.36220
 Brg#2 Span/gear...(in):   2.36220

***** Bearing Loads Calculation *****
                         <Reference>....<<Shafts.......---->
 Shaft #...................:         1
 Reference Shaft Gear#.....:         1
 Angular Location....(Degs):              .00
 Rotational Speed.....(rpm):    3565.00   21224.17
 Pitch Diameter........(in):              4.58555
 HorsePower...........(hp):     265.00    265.00
 Gear Force Components (Lbf)
 Acting on the driven shafts
 Tangential (Work) force...:              343.22
 Radial (Separating) force.:              131.35
 Axial (Thrust) force......:             -111.52
 External Load (Aero Load)
        Axial Aero Load (Lbf):            500.00
        Thrust At Radius (in):            2.45000

 Brg#1 Static Load....(Lbf):    62.0000    30.0000
        Span/Gear tooth.(in):              2.7559
        Load (X-dir)...(Lbf): -1497.3742  -143.5754
        Load (Y-dir)...(Lbf):  -233.6086   147.5264
        Load (mag.)....(Lbf):  1515.4876   205.8590
        Load (angle)..(Degs):    188.87    134.22

 Brg#2 Static Load....(Lbf):   144.0000    -5.0000
        Span/Gear tooth.(in):              2.9528
        Load (X-dir)...(Lbf):  1366.0247   274.9249
        Load (Y-dir)...(Lbf):  -315.6086   170.6908
        Load (mag.)....(Lbf):  1402.0101   323.6032
        Load (angle)..(Degs):    346.99     31.83

 Thrust Brg Loads.....(Lbf):   500.0000   388.4820
```

```
  Force acting on the Thrust Brgs
  Thrust on bull gear brg is the sum of total Aero loads
  Thrust on pinion is the force acting on the rider ring
  Aero thrusts from pinions are transmitted to bull gear
***** End of Analysis *****
```

Example 8: A 3-stages compressors

In this example, a 3-stages compressor is used to illustrate the use of this program.

Case 1: View from the air inlet side, opposite to the driver (motor). The input and outputs are shown below. One way to verify the results is consider the free-body diagram of the entire compressor and force must be balanced. In the X-Y coordinates, all the bearing reaction forces (X and Y) and summation of the gravity loads (Y) should be zero to meet the force balance requirement. The thrust load on the bull gear bearing is the summation of all the aero loads. Note that the thrust loads from the pinions acting on the bull gear are internal forces and equal to the summation of aero load and gear axial force for each pinion.
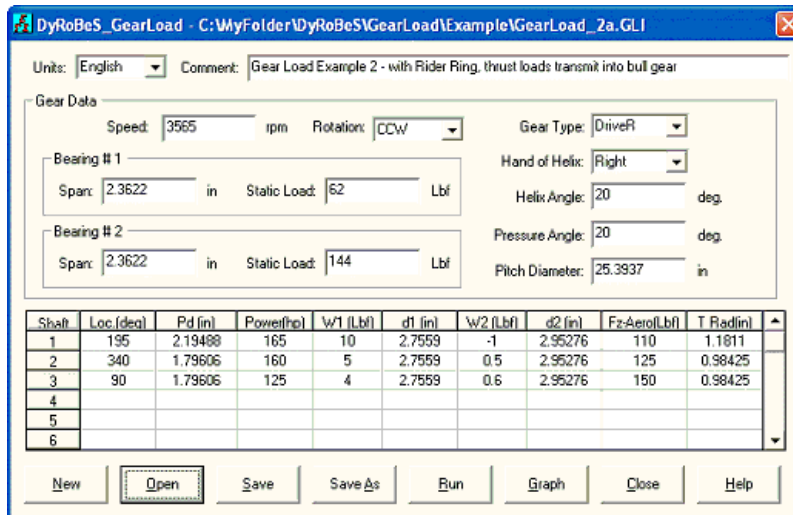

Fig 8-1

Fig 8-2

```
***** Coordinate System *****
  X-Axis to the right,  Y-Axis to the top,  Z-axis to the Observer
  Gravitational forces applied in the -Y direction
  Angle measured CCW from the +X Axis (Right Hand Rule)

  Brg#1 is the brg closest to the observer
  Brg#2 is the brg farest to the observer

***** System Description *****
  Gear Load Example 2 - with Rider Ring, thrust loads transmit into bull gear
```
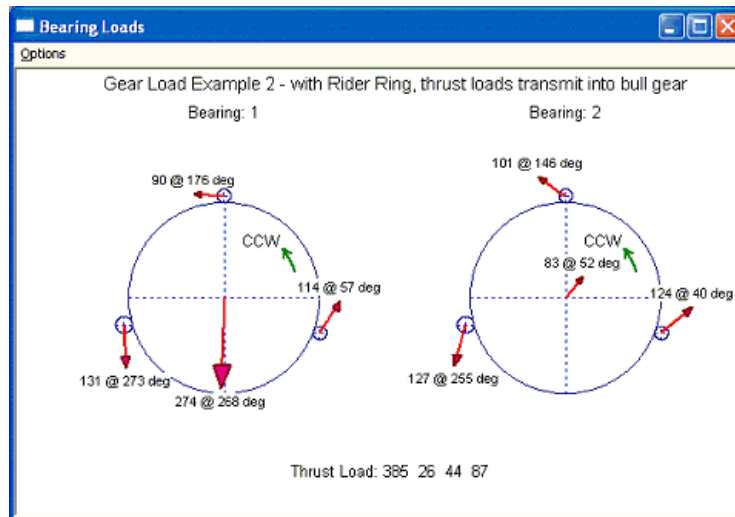
```
***** Reference Shaft Data *****
 Rotational Speed (rpm):    3565.00
 Gear Number...........:       1
 Driver/Driven Gear....:    DRIVER
 Hand of Helix.........:     RIGHT
 Direction of Rotation.:     CCW
 Helix Angle.....(Degs):    20.0000
 Pressure Angle..(Degs):    20.0000
 Pitch Diameter....(in): 25.39370
 Brg#1 Span/gear...(in):    2.36220
 Brg#2 Span/gear...(in):    2.36220

***** Bearing Loads Calculation *****
                        <Reference>....<<Shafts.......---->
 Shaft #..................:           1          2          3
 Reference Shaft Gear#.....:          1          1          1
 Angular Location....(Degs):     195.00     340.00      90.00
 Rotational Speed.....(rpm):  3565.00  41245.33   50403.96   50403.96
 Pitch Diameter........(in):             2.19488    1.79606    1.79606
 HorsePower...........(hp):   450.00     165.00     160.00     125.00
 Gear Force Components (Lbf)
 Acting on the driven shafts
 Tangential (Work) force...:             229.74     222.78     174.05
 Radial (Separating) force.:              88.99      86.29      67.41
 Axial (Thrust) force......:             -83.62     -81.09     -63.35
 External Load (Aero Load)
      Axial Aero Load (Lbf):             110.00     125.00     150.00
      Thrust At Radius (in):            1.18110     .98425     .98425

 Brg#1 Static Load....(Lbf):   62.0000    10.0000     5.0000     4.0000
       Span/Gear tooth.(in):             2.7559     2.7559     2.7559
       Load (X-dir)...(Lbf):   -8.1950     7.0965    62.2517   -90.0251
       Load (Y-dir)...(Lbf): -273.6786  -131.1237    94.9698     5.9641
       Load (mag.)....(Lbf):  273.8013   131.3155   113.5541    90.2225
       Load (angle)..(Degs):   268.28     273.10      56.76     176.21

 Brg#2 Static Load....(Lbf):  144.0000    -1.0000      .5000      .6000
       Span/Gear tooth.(in):             2.9528     2.9528     2.9528
       Load (X-dir)...(Lbf):   51.4537   -33.5887    95.0302   -84.0232
       Load (Y-dir)...(Lbf):   65.3779  -122.8232    79.3638    56.8499
       Load (mag.)....(Lbf):   83.1971   127.3332   123.8117   101.4485
       Load (angle)..(Degs):    51.80     254.71      39.87     145.92

 Thrust Brg Loads.....(Lbf):  385.0000    26.3801    43.9140    86.6516
 Force acting on the Thrust Brgs
 Thrust on bull gear brg is the sum of total Aero loads
 Thrust on pinion is the force acting on the rider ring
 Aero thrusts from pinions are transmitted to bull gear
***** End of Analysis *****
```

Case 2: View from the driver side (motor side). The input and outputs are shown below. Note that the bearing #1 is at the motor end and bearing #2 is at the air end now. The aero loads become negative (-Z direction). The results are identical to Case 1 as expected.
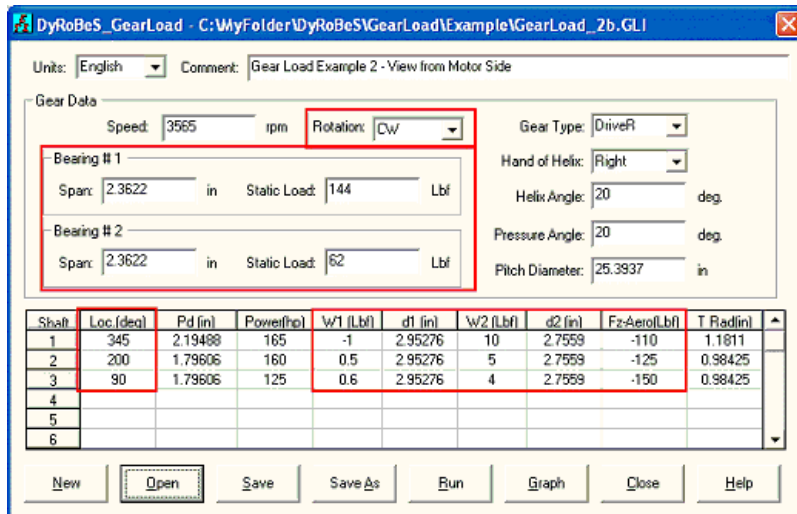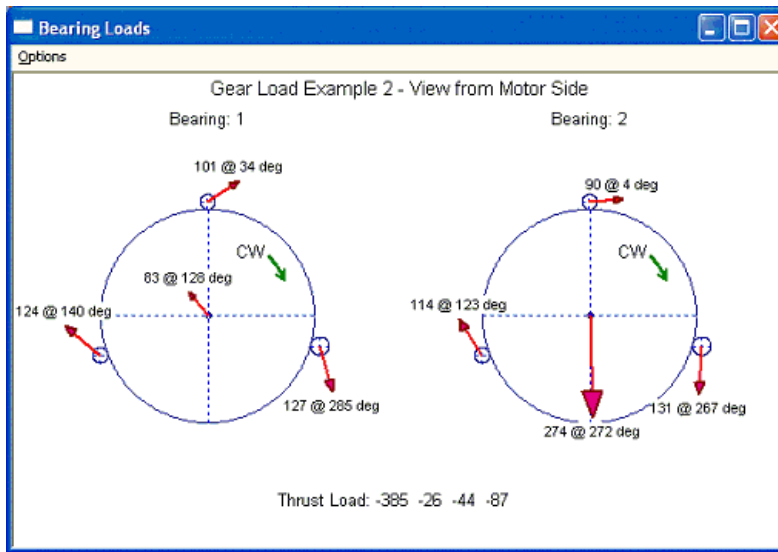

Fig 8-3

Fig 8-4

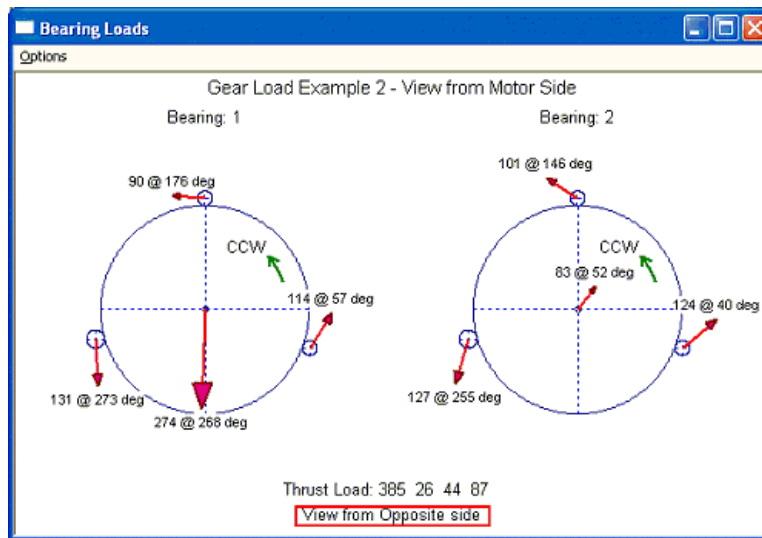Following graph is viewed from the air side.

Fig 8-5

```
***** Coordinate System *****
 X-Axis to the right,  Y-Axis to the top,  Z-axis to the Observer
 Gravitational forces applied in the -Y direction
 Angle measured CCW from the +X Axis (Right Hand Rule)

 Brg#1 is the brg closest to the observer
 Brg#2 is the brg farest to the observer

***** System Description *****
 Gear Load Example 2 - View from Motor Side

***** Reference Shaft Data *****
 Rotational Speed (rpm):    3565.00
 Gear Number...........:       1
 Driver/Driven Gear....:    DRIVER
 Hand of Helix.........:    RIGHT
 Direction of Rotation.:    CW
 Helix Angle.....(Degs):   20.0000
 Pressure Angle..(Degs):   20.0000
 Pitch Diameter....(in): 25.39370
 Brg#1 Span/gear...(in):   2.36220
 Brg#2 Span/gear...(in):   2.36220

***** Bearing Loads Calculation *****
                 <Reference>....<<Shafts.......---->
```

```
Shaft #....................:                       1         2         3
Reference Shaft Gear#.....:                        1         1         1
Angular Location....(Degs):                   345.00    200.00     90.00
Rotational Speed.....(rpm):     3565.00   41245.33  50403.96  50403.96
Pitch Diameter........(in):                  2.19488   1.79606   1.79606
HorsePower...........(hp):       450.00     165.00    160.00    125.00
Gear Force Components (Lbf)
Acting on the driven shafts
Tangential (Work) force...:                   229.74    222.78    174.05
Radial (Separating) force.:                    88.99     86.29     67.41
Axial (Thrust) force......:                   -83.62    -81.09    -63.35
External Load (Aero Load)
        Axial Aero Load (Lbf):               -110.00   -125.00   -150.00
        Thrust At Radius (in):               1.18110    .98425    .98425

Brg#1 Static Load....(Lbf):     144.0000    -1.0000     .5000     .6000
        Span/Gear tooth.(in):              2.9528    2.9528    2.9528
        Load (X-dir)...(Lbf):   -51.4537    33.5887  -95.0302   84.0232
        Load (Y-dir)...(Lbf):    65.3779  -122.8232   79.3638   56.8499
        Load (mag.)....(Lbf):    83.1971   127.3332  123.8117  101.4485
        Load (angle)..(Degs):     128.20    285.29    140.13     34.08

Brg#2 Static Load....(Lbf):      62.0000    10.0000    5.0000    4.0000
        Span/Gear tooth.(in):              2.7559    2.7559    2.7559
        Load (X-dir)...(Lbf):     8.1950    -7.0965  -62.2517   90.0251
        Load (Y-dir)...(Lbf):  -273.6786  -131.1237   94.9698    5.9641
        Load (mag.)....(Lbf):   273.8013   131.3155  113.5541   90.2225
        Load (angle)..(Degs):     271.72    266.90    123.24      3.79

Thrust Brg Loads.....(Lbf):    -385.0000   -26.3801  -43.9140  -86.6516
Force acting on the Thrust Brgs
Thrust on bull gear brg is the sum of total Aero loads
Thrust on pinion is the force acting on the rider ring
Aero thrusts from pinions are transmitted to bull gear
***** End of Analysis *****
```

Case 3: In this case, the thrust bearings are used for each shaft. Inputs and Outputs are shown below. The thrust load on the bull gear is the sum of all the gear axial forces from 3 pinions. The thrust load on the pinion is the sum of aero load and gear axial force for each pinion.
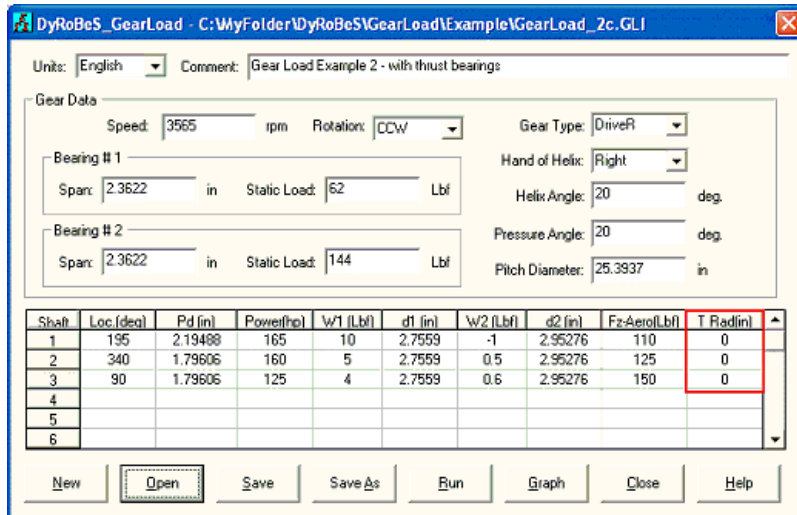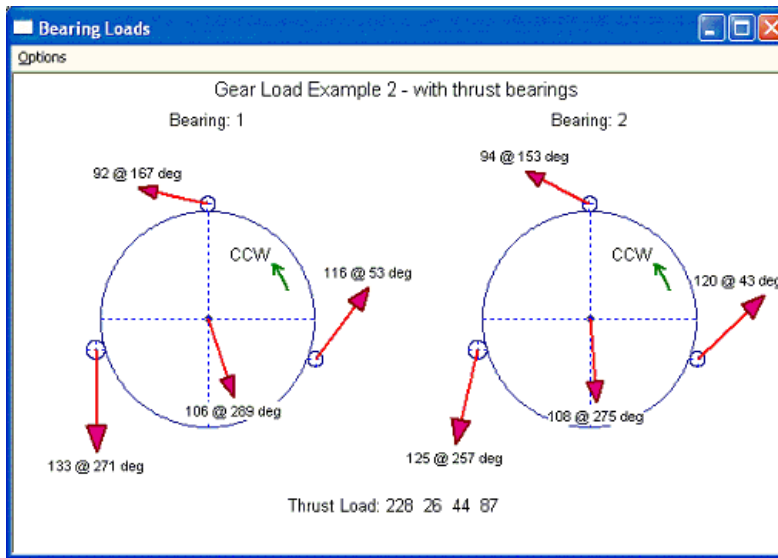

Fig 8-6

Fig 8-7

```
***** Coordinate System *****
 X-Axis to the right,  Y-Axis to the top,  Z-axis to the Observer
 Gravitational forces applied in the -Y direction
 Angle measured CCW from the +X Axis (Right Hand Rule)

 Brg#1 is the brg closest to the observer
 Brg#2 is the brg farest to the observer

***** System Description *****
 Gear Load Example 2 - with thrust bearings

***** Reference Shaft Data *****
 Rotational Speed (rpm):    3565.00
 Gear Number...........:       1
 Driver/Driven Gear....:    DRIVER
 Hand of Helix.........:    RIGHT
 Direction of Rotation.:    CCW
 Helix Angle.....(Degs):   20.0000
 Pressure Angle..(Degs):   20.0000
 Pitch Diameter....(in):  25.39370
 Brg#1 Span/gear...(in):   2.36220
 Brg#2 Span/gear...(in):   2.36220

***** Bearing Loads Calculation *****
                        <Reference>....<<Shafts.......---->
 Shaft #...................:                1         2         3
 Reference Shaft Gear#.....:                1         1         1
 Angular Location....(Degs):           195.00    340.00     90.00
 Rotational Speed.....(rpm):  3565.00  41245.33  50403.96  50403.96
 Pitch Diameter........(in):            2.19488   1.79606   1.79606
 HorsePower............(hp):   450.00   165.00    160.00    125.00
 Gear Force Components (Lbf)
 Acting on the driven shafts
 Tangential (Work) force...:            229.74    222.78    174.05
 Radial (Separating) force.:             88.99     86.29     67.41
 Axial (Thrust) force......:            -83.62    -81.09    -63.35
 External Load (Aero Load)
      Axial Aero Load (Lbf):            110.00    125.00    150.00
      Thrust At Radius (in):            .00000    .00000    .00000


 Brg#1 Static Load....(Lbf):  62.0000   10.0000    5.0000    4.0000
       Span/Gear tooth.(in):             2.7559    2.7559    2.7559
       Load (X-dir)...(Lbf):  33.9240    1.8245   69.3664  -90.0251
       Load (Y-dir)...(Lbf): -100.7027 -132.5363   92.3802   20.9040
       Load (mag.)....(Lbf): 106.2633  132.5488  115.5240   92.4202
       Load (angle)..(Degs): 288.62    270.79     53.10    166.93

 Brg#2 Static Load....(Lbf): 144.0000   -1.0000    .5000     .6000
       Span/Gear tooth.(in):             2.9528    2.9528    2.9528
       Load (X-dir)...(Lbf):   9.3347  -28.3168   87.9154  -84.0232
       Load (Y-dir)...(Lbf): -107.5980 -121.4105   81.9534   41.9100
       Load (mag.)....(Lbf): 108.0021  124.6690  120.1893   93.8954
       Load (angle)..(Degs): 274.96    256.87     42.99    153.49
```

```
Thrust Brg Loads.....(Lbf):   228.0543    26.3801    43.9140    86.6516
Force acting on the Thrust Brgs
Each rotor has its own thrust bearing
***** End of Analysis *****
```